

## JEE I NEET I Foundation

# Motion 



## Section - A

1. Four identical particles of equal masses 1 kg made to move along the circumference of a circle of radius 1 m under the action of their own mutual gravitational attraction. The speed of each particle will be -
(1) $\frac{\sqrt{(1+2 \sqrt{2}) G}}{2}$
(2) $\sqrt{G(1+2 \sqrt{2})}$
(3) $\sqrt{\frac{G}{2}(2 \sqrt{2}-1)}$
(4) $\sqrt{\frac{G}{2}(1+2 \sqrt{2})}$

Sol. (1)

$\Rightarrow$ By resolving force $F_{2}$, we get
$\Rightarrow F_{1}+F_{2} \cos 45^{\circ}+F_{2} \cos 45^{\circ}$
$\Rightarrow F_{1}+2 F_{2} \cos 45^{\circ}=F_{c}$
$\mathrm{F}_{\mathrm{c}}=$ centripital force $=\frac{\mathrm{MV}^{2}}{\mathrm{R}}$
$\Rightarrow \frac{G M^{2}}{(2 R)^{2}}+\left[\frac{2 G M^{2}}{(\sqrt{2 R})^{2}} \cos 45^{\circ}\right]=\frac{M V^{2}}{R}$
$\Rightarrow \frac{G M^{2}}{4 R^{2}}+\frac{2 G M^{2}}{2 \sqrt{2} R^{2}}=\frac{M V^{2}}{R}$
$\Rightarrow \frac{\mathrm{GM}}{4 \mathrm{R}}+\frac{\mathrm{GM}}{\sqrt{2} \cdot \mathrm{R}}=\mathrm{V}^{2}$
$\Rightarrow V=\sqrt{\frac{G M}{4 R}+\frac{G M}{\sqrt{2} \cdot R}}$
$\Rightarrow \mathrm{V}=\sqrt{\frac{\mathrm{GM}}{\mathrm{R}}\left[\frac{1+2 \sqrt{2}}{4}\right]}$
$\Rightarrow \mathrm{V}=\frac{1}{2} \sqrt{\frac{\mathrm{GM}}{\mathrm{R}}(1+2 \sqrt{2})}$
(given : mass $=1 \mathrm{~kg}$, radius $=1 \mathrm{~m}$ )
$\Rightarrow \mathrm{V}=\frac{1}{2} \sqrt{\mathrm{G}(1+2 \sqrt{2})}$
2. Consider two satellites $\mathrm{S}_{1}$ and $\mathrm{S}_{2}$ with periods of revolution 1 hr . and 8 hr . respectively revolving around a planet in circular orbits. The ratio of angular velocity of satellite $S_{1}$ to the angular velocity of satellite $S_{2}$ is -
(1)8: 1
(2) $1: 8$
(3)2: 1
(4) $1: 4$

Sol. (1)
We know that $\omega=\frac{2 \pi}{T}$
given : Ratio of time period
$\frac{T_{1}}{T_{2}}=\frac{1}{8}$
$\Rightarrow \omega \propto \frac{1}{\mathrm{~T}}$
$\Rightarrow \frac{\omega_{1}}{\omega_{2}}=\frac{\mathrm{T}_{2}}{\mathrm{~T}_{1}}$
$\Rightarrow \frac{\omega_{1}}{\omega_{2}}=\frac{8}{1}$
$\Rightarrow \omega_{1}: \omega_{2}=8: 1$
3. $n$ mole of a perfect gas undergoes a cyclic process ABCA (see figure) consisting of the following processes -
$A \rightarrow B$ : Isothermal expansion at temperature $T$ so that the volume is doubled from $V_{1}$ to $V_{2}=2 V_{1}$ and pressure changes from $P_{1}$ to $P_{2}$.
$B \rightarrow C$ : Isobaric compression at pressure $P_{2}$ to initial volume $V_{1}$.
$C \rightarrow A$ : Isochoric change leading to change of pressure from $P_{2}$ to $P_{1}$.
Total workdone in the complete cycle ABCA is -

(1) 0
(2) $n R T\left(\ln 2+\frac{1}{2}\right)$
(3) nRTIn2
(4) nRT $\left(\ln 2-\frac{1}{2}\right)$

## Sol. (4)


$A \rightarrow B=$ isotheraml process
$B \rightarrow C=$ isobaric process
$C \rightarrow A=$ isochoric process
also, $\mathrm{V}_{2}=2 \mathrm{~V}_{1}$
work done by gas in the complete cycle ABCA is -
$\Rightarrow \mathrm{w}=\mathrm{w}_{\mathrm{AB}}+\mathrm{w}_{\mathrm{BC}}+\mathrm{w}_{\mathrm{CA}}$
$\Rightarrow \mathrm{w}_{\mathrm{CA}}=0$, as isochoric process
$\Rightarrow W_{A B}=2 P_{1} V_{1} \ln \left(\frac{v_{2}}{v_{1}}\right)=2 n R T \ln (2)$
$\Rightarrow W_{B C}=P_{2}\left(V_{1}-V_{2}\right)=P_{2}\left(V_{1}-2 V_{1}\right)=-P_{2} V_{1}=-n R T$
$\Rightarrow$ Now put the value of $W_{A B}, W_{B C}$ and $W_{C A}$ in equation, we get
$\Rightarrow \mathrm{w}=2 \mathrm{nRT} \ln (2)-\mathrm{nRT}+0$
$\Rightarrow \mathrm{w}=\mathrm{nRT}[2 \ln (2)-1]$
$\Rightarrow \mathrm{w}=\mathrm{nRT}\left[\ln (2)-\frac{1}{2}\right]$
4. Two equal capacitors are first connected in series and then in parallel. The ratio of the equivalent capacities capacities in the two cases will be -
(1)2 : 1
(2)1: 4
(3)4: 1
(4) $1: 2$

## Sol. (2)

Given that first connection

$\Rightarrow \frac{1}{\mathrm{C}_{12}}=\frac{1}{\mathrm{C}}+\frac{1}{\mathrm{C}} \Rightarrow \mathrm{C}_{12}=\frac{\mathrm{C}}{2}$

## Second connection

$\mathrm{C}_{34}=\mathrm{C}+\mathrm{C}=2 \mathrm{C}$

Now, the ratio of equivalent capacities in the two cases will be -
$\Rightarrow \frac{C_{12}}{C_{34}}=\frac{C / 2}{2 C} \Rightarrow \frac{C_{12}}{C_{34}}=\frac{1}{4}$

5. A cell $E_{1}$ of emf 6 V and internal resistance $2 \Omega$ is connected with another cell $E_{2}$ of emf 4 V and internal resistance $8 \Omega$ (as shown in the figure). The potential difference across points $X$ and $Y$ is -

(1)3.6V
(2)10.0V
(3) 5.6 V
(4) 2.0 V

Sol. (3)

emf of $E_{1}=6 v$
$r_{1}=2 \Omega$
emf of $E_{2}=4 \Omega$
$r_{2}=8 \Omega$
$\left|v_{x}-v_{y}\right|=$ potential difference across points $x$ and $y$
$\mathrm{E}_{\text {eff }}=6-4=2 \mathrm{~V}$
$R_{\text {eq }}=2+8=10 \Omega$
So, current in the circuit will be
$\Rightarrow I=\frac{E_{\text {eff }}}{R_{\text {eq }}} \Rightarrow I=\frac{2}{10}=0.2 \mathrm{~A}$
Now, potential difference across points $X$ and $Y$ is
$\left|v_{x}-v_{y}\right|=E+i R$
$\Rightarrow\left|v_{x}-v_{y}\right|=4+0.2 \times 8=5.6 \mathrm{~V}$
$\Rightarrow\left|v_{x}-v_{y}\right|=5.6 v$
6. If $Y, K$ and $\eta$ are the values of Young's modulus, bulk modulus and modulus of rigidity of any material respectively. Choose the correct relation for these parameters.
$(1) K=\frac{Y \eta}{9 \eta-3 Y} N / m^{2}$
(2) $\eta=\frac{3 Y K}{9 K+Y} N / m^{2}$
$(3) Y=\frac{9 K \eta}{3 K-\eta} N / m^{2}$
(4) $Y=\frac{9 K \eta}{2 \eta+3 K} N / m^{2}$

Sol. (1)
$\Rightarrow y=3 k(1-2 \sigma)$
$\Rightarrow \sigma=\frac{1}{2}\left(1-\frac{\mathrm{y}}{3 \mathrm{k}}\right)$
$\Rightarrow y=2 \eta(1+\sigma)$
$\Rightarrow \sigma=\frac{y}{2 \eta}-1$
by comparing equation (1) and (2), we get
$\Rightarrow \frac{y}{2 \eta}-1=\frac{1}{2}\left(1-\frac{y}{3 k}\right)$
$\Rightarrow \frac{\mathrm{y}}{\eta}-2=1-\frac{\mathrm{y}}{3 \mathrm{k}}$
$\Rightarrow \frac{\mathrm{y}}{\eta}=1+2-\frac{\mathrm{y}}{3 \mathrm{k}} \Rightarrow \frac{\mathrm{y}}{\eta}=3-\frac{\mathrm{y}}{3 \mathrm{k}}$
$\Rightarrow \frac{y}{3 k}=3-\frac{y}{\eta} \Rightarrow \frac{y}{3 k}=\frac{3 \eta-y}{\eta}$
$\Rightarrow k=\frac{\eta y}{9 \eta-3 y}$
7. Two stars of masses $m$ and $2 m$ at a distance $d$ rotate about their common centre of mass in free space. The period of revolution is -
(1) $2 \pi \sqrt{\frac{d^{3}}{3 G m}}$
(2) $\frac{1}{2 \pi} \sqrt{\frac{3 G m}{d^{3}}}$
(3) $\frac{1}{2 \pi} \sqrt{\frac{d^{3}}{3 G m}}$
(4) $2 \pi \sqrt{\frac{3 G m}{d^{3}}}$

Sol. (1)

$\Rightarrow \frac{G(m)(2 m)}{d^{2}}=m \omega^{2} \times \frac{2 d}{3}$
$\Rightarrow \frac{2 \mathrm{Gm}}{\mathrm{d}^{2}}=\omega^{2} \times \frac{2 \mathrm{~d}}{3}$
$\Rightarrow \omega^{2}=\frac{3 G m}{d^{3}}$
$\Rightarrow \omega=\sqrt{\frac{3 G m}{d^{3}}}$
we know that, $\omega=\frac{2 \pi}{\mathrm{~T}}$ so $\mathrm{T}=\frac{2 \pi}{\omega}$
$\Rightarrow \mathrm{T}=\frac{2 \pi}{\sqrt{\frac{3 G m}{d^{3}}}} \Rightarrow \mathrm{~T}=2 \pi \sqrt{\frac{\mathrm{~d}^{3}}{3 \mathrm{Gm}}}$
8. If the velocity-time graph has the shape $A M B$, what would be the shape of the corresponding acceleration-time graph ?

(1)

(2)

(3)

(4)


Sol. (1)

$a=\frac{d v}{d t}=$ slope of $(v-t)$ curve

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If $m=+v e$, then equation of straight line is
$y=m x+c \Rightarrow v=m t+c$ (for MB)
If $m=-v e$, then equation of straight line is
$y=-m x+c \Rightarrow v=-m t+c$ (for $A M)$
If we differentiate equation (1) and (2), we get
$a_{\text {MB }}=+v e=m$
$a_{\text {AM }}=-v e=-m$, so graph of (a-t) will be

9. Given below are two statements :

Statement - I: Two photons having equal linear momenta have equal wavelengths.
Statement-II: If the wavelength of photon is decreased, then the momentum and energy of a photon will also decrease.
In the light of the above statements, choose the correct answer from the options given below.
(1)Statemnet-I is false but Statement-II is true
(2)Both Statement-I and Statement-II are true
(3)Both Statement-I and Statement-II are false
(4) Statement-I is true but Statement-II is false

## Sol. (4)

By theory
10. A current through a wire depends on time as $i=\alpha_{0} t+\beta t^{2}$
where $\alpha_{0}=20 \mathrm{~A} / \mathrm{s}$ and $\beta=8 \mathrm{As}^{-2}$. Find the charge crossed through a section of the wire in 15 s .
(1) 2100 C
(2) 260 C
(3) 2250 C
(4) 11250 C

## Sol. (4)

given : $i=\alpha_{0} t+\beta t^{2}$
$\alpha=20 \mathrm{~A} / \mathrm{s}$ and $\beta=8 \mathrm{As}^{-2}$
$t=15 \mathrm{sec}$
we know that, $\mathrm{i}=\frac{\mathrm{dq}}{\mathrm{dt}} \Rightarrow \int_{0}^{\mathrm{t}} \mathrm{idt}=\int_{0}^{\mathrm{Q}} \mathrm{dq}$
$\Rightarrow \int_{0}^{15}\left(\alpha_{0} t+\beta t^{2}\right) d t=\int_{0}^{Q} d q$
$\Rightarrow Q=\left[\frac{\alpha_{0} t^{2}}{2}+\frac{\beta t^{3}}{3}\right]_{0}^{15}$
$\Rightarrow Q=\frac{20 \times 15 \times 15}{2}+\frac{8 \times 15 \times 15 \times 15}{3}-0$
$\Rightarrow Q=11250 C$
11. match List I with List II

List-I
(a) Isothermal
(b) Isochoric
(i) Pressure constant
(c) Adiabatic
(ii) Temperature constant
(d) Isobaric
(iii) Volume constant

## List-II

Choose the correct answer from the options given below -
(1)(a) - (ii), (b) - (iv), (c) - (iii), (d) - (i)
(2)(a) - (ii), (b) - (iii), (c) - (iv), (d) - (i)
(3)(a) - (i), (b) - (iii), (c) - (ii), (d) - (iv)
(4) (a) - (iii), (b) - (ii), (c) - (i), (d) - (iv)

## Sol. (2)

(a) $\rightarrow$ (ii), (b) $\rightarrow$ (iii),
(c) $\rightarrow$ (iv),
(d) $\rightarrow$ (i),

By theory
In isothermal process, temperature is constant.
In isochoric process, volume is constant.
In adiabatic process, heat content is constant.
In isobaric process, pressure is constant.
12. In the given figure, the energy levels of hydrogen atom have been shown along with some transitions marked $A, B, C, D$ and $E$.
The transitions $A, B$ and $C$ respectively represents -

(1)The series limit of Lyman series, third member of balmer series and second member of paschen series
(2)The first member of the Lyman series, third member of Balmer series and second member of paschen series

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(3)The ionization potential of hydrogen, second member of Balmer series and third member of Paschen series
(4) The series limit of Lyman series, second memebr of Balmer series and second member of Paschen series.
Sol. (1)
A $\rightarrow$ series limit of lyman.
$B \rightarrow 3^{\text {rd }}$ member of Balmer series.
$C \rightarrow 2^{\text {nd }}$ member of Paschen series.
13. The focal length $f$ is related to the radius of curvature $r$ of the spherical convex mirror by -
(1) $f=r$
(2) $f=-\frac{1}{2} r$
(3) $f=+\frac{1}{2} r$
(4) $f=-r$

Sol. (3)


So, $\frac{R}{2}=f$
$F=+\frac{1}{2} R$
14. Moment of inertia (M.I.) of four bodies, having same mass and radius, are reported as $I_{1}=$ M.I. of thin circular ring about its diameter,
$I_{2}=$ M.I. of circular disc about an axis perpendicular to disc and going through the centre,
$I_{3}=$ M.I. of solid cylinder about its axis and
$I_{4}=$ M.I. of solid sphere about its diameter.
Then :-
(1) $I_{1}=I_{2}=I_{3}<I_{4}$
(2) $I_{1}+I_{2}=I_{3}+\frac{5}{2} I_{4}$
(3) $I_{1}+I_{3}<I_{2}+I_{4}$
(4) $I_{1}=I_{2}=I_{3}>I_{4}$

Sol. (4)
Given $\Rightarrow I_{1}=$ M.I. of thin circular ring about its diameter
$I_{2}=$ M.I. circular disc about an axis perpendicular to disc and going through the centre.
$I_{3}=$ M.I. of solid cylinder about its axis
$I_{4}=$ M.I. of solid sphere about its diameter we know that,
$I_{1}=\frac{M R^{2}}{2}, I_{2}=\frac{M R^{2}}{2}, I_{3}=\frac{M R^{2}}{2}$
$\mathrm{I}_{4}=\frac{2}{5} M R^{2}$
So, $I_{1}=I_{2}=I_{3}>I_{4}$
15. The workdone by a gas molecule in an isolated system is given by, $W=\alpha \beta^{2} e^{-\frac{x^{2}}{\alpha k T}}$, where $x$ is the displacement, $k$ is the Boltzmann constant and $T$ is the temperature. $\alpha$ and $\beta$ are constants. Then the dimensions of $\beta$ will be -
(1) $\left[M^{0} \mathrm{LT}^{0}\right]$
(2) $\left[M^{2} L T^{2}\right]$
(3) $\left[\mathrm{MLT}^{-2}\right]$
(4) $\left[\mathrm{ML}^{2} \mathrm{~T}^{-2}\right]$

## Sol. (3)

given : work $=\alpha \cdot \beta^{2} \cdot e^{-\frac{x^{2}}{a, k T}}$
$\mathrm{k}=$ boltzmann constant
$\mathrm{T}=$ temperature
$\mathrm{x}=$ displacement
we know that, $\frac{x^{2}}{\alpha . \text { k. T }}=$ dimensionless
$\left[\frac{\mathrm{x}^{2}}{\alpha . k . T}\right]=\left[\mathrm{M}^{0} \mathrm{~L}^{0} \mathrm{~T}^{0}\right]$
$[\alpha]=\left[\frac{L^{2}}{K . T}\right]$
$\Rightarrow[K]=\left[M^{1} L^{2} T^{-2} K^{-1}\right]$
$[\mathrm{T}]=[\mathrm{K}]$
$\Rightarrow[\alpha]=\left[\frac{\mathrm{L}^{2}}{\mathrm{M}^{1} \mathrm{~L}^{2} \mathrm{~T}^{-2} \mathrm{~K}^{-1} \times \mathrm{K}}\right] \Rightarrow[\alpha]=\left[\mathrm{M}^{-1} \mathrm{~T}^{2}\right]$
$\Rightarrow \omega=\alpha \cdot \beta^{2}$
$\Rightarrow \frac{\left[\mathrm{M}^{1} \mathrm{~L}^{1} \mathrm{~T}^{-2}\right]\left[\mathrm{L}^{-1}\right]}{\left[\mathrm{M}^{-1} \mathrm{~T}^{2}\right]}=\left[\beta^{2}\right]=\left[\mathrm{M}^{2} \mathrm{~L}^{2} \mathrm{~T}^{-4}\right]$
$[\beta]=\left[\mathrm{MLT}^{-2}\right]$
16. If an emitter current is changed by 4 mA , the collector current changes by 3.5 mA . The value of $\beta$ will be -
(1)7
(2) 0.875
(3) 0.5
(4) 3.5

Sol. (1)
Given :
$\Delta \mathrm{I}_{\mathrm{E}}=4 \mathrm{~mA}$
$\Delta \mathrm{I}_{\mathrm{C}}=3.5 \mathrm{~mA}$
we know that, $\alpha=\frac{\Delta \mathrm{I}_{\mathrm{C}}}{\Delta \mathrm{I}_{\mathrm{E}}}$
$\Rightarrow \alpha=\frac{3.5}{4}=\frac{7}{8}$
Also, $\beta=\frac{\alpha}{1-\alpha}$, so
$\beta=\frac{\frac{7}{8}}{1-\frac{7}{8}}=\frac{7}{1}$
$\beta=7$
17. In a Young's double slit experiment, the width ofthe one of the slit is three times the other slit. The amplitude of the light coming from a slit is proportional to the slit-width. Find the ratio of the maximum to the minimum intensity in the interference pattern.
(1)4: 1
(2)2: 1
(3)3: 1
(4) $1: 4$

## Sol. (1)


given : $\omega_{2}=3 \omega_{1}$
also, $A \propto \omega$
$\frac{\omega_{1}}{\omega_{2}}=\frac{1}{3}$
Assume $\omega_{1}=x, \omega_{2}=3 x$
we know that

$$
\begin{aligned}
& I_{\max }=\left(A_{1}+A_{2}\right)^{2}, \text { and } \\
& I_{\min }=\left(A_{1}-A_{2}\right)^{2}
\end{aligned}
$$

$\frac{\mathrm{A}_{1}}{\mathrm{~A}_{2}}=\frac{\omega_{1}}{\omega_{2}}$
from equation (2) we can say that
$A_{1}=A$ and $A_{2}=3 A$
Now, $\frac{I_{\text {max }}}{I_{\text {min }}}=\frac{(A+3 A)^{2}}{(A-3 A)^{2}}=\frac{16 A^{2}}{4 A^{2}}=\frac{4}{1}$
$\Rightarrow \frac{\mathrm{I}_{\text {max }}}{\mathrm{I}_{\text {min }}}=\frac{4}{1}$
18. In the given figure, a mass $M$ is attached to a horizontal spring which is fixed on one side to a rigid support. The spring constant of the spring is $k$. The mass oscillates on a frictionless surface with time period $T$ and amplitude $A$. When the mass is in equilibrium position, as shown in the figure, another mass $m$ is gently fixed upon it. The new amplitude of oscillation will be -

(1)A $\sqrt{\frac{M}{M+m}}$
(2) $A \sqrt{\frac{M}{M-m}}$
(3) $A \sqrt{\frac{M-m}{M}}$
(4) $A \sqrt{\frac{M+m}{M}}$

Sol. (1)


Before placing

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After placing
We know that $\omega=\sqrt{\frac{k}{m}}$ and $\omega_{i}=\sqrt{\frac{k}{M}} \quad A_{i}=A$
Also, momentum is conserved just before and just after the block of mass ( $m$ ) is placed because there is no implusive force. So -
$M A_{i} \omega_{i}=(M+m) v^{\prime}$
$v^{\prime}=\frac{M A_{i} \omega_{i}}{(M+m)} \Rightarrow v^{\prime}=A_{f} \omega_{f}$
$\frac{M A \omega_{i}}{(M+m)}=A_{f} \sqrt{\frac{K}{(M+m)}}$
$\Rightarrow \frac{M A \sqrt{\frac{K}{M}}}{M+m} \times \sqrt{\frac{M+m}{K}}=A_{f}$
$\Rightarrow A_{f}=A \sqrt{\frac{M}{(M+m)}}$
19. A cube of side ' $a$ ' has point charges $+Q$ located at each of its vertices except at the origin where the charge is -Q . The electric field at the centre of cube is :

(1) $\frac{2 \mathrm{Q}}{3 \sqrt{3} \pi \varepsilon_{0} \mathrm{a}^{2}}(\hat{\mathrm{x}}+\hat{\mathrm{y}}+\hat{\mathrm{z}})$
(2) $\frac{Q}{3 \sqrt{3} \pi \varepsilon_{0} a^{2}}(\hat{x}+\hat{y}+\hat{z})$
(3) $\frac{-2 Q}{3 \sqrt{3} \pi \varepsilon_{0} a^{2}}(\hat{x}+\hat{y}+\hat{z})$
(4) $\frac{-Q}{3 \sqrt{3} \pi \varepsilon_{0} a^{2}}(\hat{x}+\hat{y}+\hat{z})$

## Sol. (3)



If only $+Q$ charges are placedat the corners of cube of side a then electric field at the centre of the cube will be zero.
But in the given condition one (-Q) is placed at one corner of cube so here
$E_{1}=E_{6}, E_{2}=E_{5}$ and $E_{3}=E_{8}$ (So it will cancel out each other so electric field at centre is due to $\mathrm{Q}_{4}$ and $\mathrm{Q}_{7}$.
Here electric field at centre $=2$ (E.f.) $)_{4}$
As, $\left|E_{4}\right|=\left|E_{7}\right|$
$(\mathrm{E} . \mathrm{F})_{\mathrm{c}}=\frac{2 \mathrm{kQ}}{\left(\frac{\sqrt{3} \mathrm{a}}{2}\right)^{2}}=\frac{8 \mathrm{KQ}}{3 \mathrm{a}^{2}} \quad\left\{\because \mathrm{~K}=\frac{1}{4 \pi \varepsilon_{0}}\right\}$
$(\mathrm{E} . \mathrm{F})_{\mathrm{c}}=\frac{2 \mathrm{Q}}{3 \mathrm{a}^{2} \pi \varepsilon_{0}}$
In vector form $\Rightarrow \vec{E}=\frac{-2 Q}{3 a^{2} \pi \varepsilon_{0}} \times\left(\frac{\hat{x}+\hat{y}+\hat{z}}{\sqrt{3}}\right)$
20. Each side of a box made of metal sheet in cubic shape is ' $a$ ' at room temperature ' $T$ ', the coefficient of linear expansion of the metal sheet is ' $\alpha$ '. The metal sheet is heated uniformly, by a small temperature $\Delta \mathrm{T}$, so that its new temeprature is $\mathrm{T}+\Delta \mathrm{T}$. Calculate theincrease in the volume of the metal box-
(1) $\frac{4}{3} \pi a^{3}{ }_{\alpha \Delta T}$
(2) $4 \pi a^{3} \alpha \Delta T$
(3) $3 a^{3} \alpha \Delta T$
(4) $4 a^{3} \alpha \Delta T$

Sol. (3)
volume expansion $\gamma=3 \alpha$
$\frac{\Delta \mathrm{V}}{\mathrm{V}}=\gamma \Delta \mathrm{T}$
$\Delta \mathrm{V}=\mathrm{V} \cdot \gamma \Delta \mathrm{T}$
$\Delta V=a^{3} .3 \alpha \Delta T$

## SECTION-B

1. A resonance circuit having inductance and resistance $2 \times 10^{-4} \mathrm{H}$ and $6.28 \Omega$ respectively oscillates at 10 MHz frequency. The value of quality factor of this resonator is $\qquad$ .
[ $\pi=3.14$ ]
Sol. 2000
Given : $\mathrm{R}=6.28 \Omega$
$\mathrm{f}=10 \mathrm{MHz}$
$\mathrm{L}=2 \times 10^{-4}$ Henry
we know that quality factor Q is given by
$\Rightarrow Q=\frac{X_{L}}{R}=\frac{\omega L}{R}$
also, $\omega=2 \pi f$, so
$\Rightarrow \mathrm{Q}=\frac{2 \pi \mathrm{fL}}{\mathrm{R}}$
$\Rightarrow \mathrm{Q}=\frac{2 \pi \times 10 \times 10^{6} \times 2 \times 10^{-4}}{6.28}=2000$
$Q=2000$
2. A ball with a speed of $9 \mathrm{~m} / \mathrm{s}$ collides with another identical ball at rest. After thecollision, the direction of each ball makes an angle of $30^{\circ}$ with the original direction. The ratio of velocities of the balls after collision is $x: y$, where $x$ is $\qquad$ .
Sol. 1


Momentum is conserved just before and just after the collision in both $x-y$ direction.
In $y$-direction
$p_{i}=0$
$P_{f}=m \times \frac{1}{2} v_{1}-m \times \frac{1}{2} v_{2}$
$p_{i}=p_{f}$, so
$=\frac{m v_{1}}{2}-\frac{m v_{2}}{2}=0$
$\Rightarrow \frac{\mathrm{mv}_{1}}{2}=\frac{\mathrm{mv}}{2} \Rightarrow \mathrm{v}_{1}=\mathrm{v}_{2}$
$\frac{v_{1}}{v_{2}}=1$
3. An audio signal $v_{m}=20 \sin 2 \pi(1500 t)$ amplitude modulates a carrier $v_{c}=80 \sin 2 \pi(100,000 t)$. The value of percent modulation is $\qquad$ .
Sol. 25
Given $: v_{m}=20 \sin \left[100 \pi t+\frac{\pi}{4}\right]$
$v_{c}=80 \sin \left[10^{4} \pi t+\frac{\pi}{6}\right]$
we know that, modulation index $=\frac{A_{m}}{A_{c}}$
from given equations, $A_{m}=20$ and $A_{c}=80$
percentage modulation index $=\frac{A_{m}}{A_{c}} \times 100$
$\Rightarrow \frac{20}{80} \times 100=25 \%$
The value of percentage modulation index is
$=25$
4. The coefficient of static friction between a wooden block of mass 0.5 kg and a vertical rough wall is 0.2. The magnitude of horizontal force that should be applied on the block to keep it adhere to the wall will be $\qquad$ N.
$\left[\mathrm{g}=10 \mathrm{~ms}^{-2}\right.$ ]
Sol. 25


Given : $\mu_{\mathrm{s}}=0.2$

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$\mathrm{m}=0.5 \mathrm{~kg}$
$\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$
we know that
$\mathrm{f}_{\mathrm{s}}=\mu \mathrm{N}$ and
To keep the block adhere to the wall
here $\mathrm{N}=\mathrm{F}$
$\mathrm{f}_{\mathrm{s}}=\mathrm{mg}$
from equation (1), (2), and (3), we get
$\Rightarrow \mathrm{mg}=\mu \mathrm{F}$
$\Rightarrow F=\frac{\mathrm{mg}}{\mu} \Rightarrow F=\frac{0.5 \times 10}{0.2}$
$\mathrm{F}=25 \mathrm{~N}$
5. An inclined plane is bent in such a way that the vertical cross-section is given by $y=\frac{x^{2}}{4}$ where $y$ is in vertical and $x$ in horizontal direction. If the upper surface of this curved plane is rough with coefficient of friction $\mu=0.5$, the maximum height in cm at which a stationary block will not slip downward is $\qquad$ cm.

Sol. 25

given
$y=\frac{x^{2}}{4}$
$\mu=0.5$
condition for block will not slip downward
$\mathrm{mg} \sin \theta=\mu \mathrm{mg} \cos \theta$

$\Rightarrow \tan \theta=\mu$
and we know that
$\Rightarrow \tan \theta=\frac{\mathrm{dy}}{\mathrm{dx}}$
$\Rightarrow \frac{\mathrm{dy}}{\mathrm{dx}}=\mu \Rightarrow \frac{\mathrm{x}}{2}=0.5$

$$
\left[\begin{array}{l}
y=\frac{x^{2}}{4} \\
\frac{d y}{d x}=\frac{x}{2}
\end{array}\right]
$$

$\Rightarrow x=1$,
put $x=1$ in equation $y=x^{2} / 4$
$\Rightarrow y=\frac{(1)^{2}}{4} \Rightarrow y=\frac{1}{4} \Rightarrow y=0.25$
$y=25 \mathrm{~cm}$
6. An electromagnetic wave of frequency 5 GHz , is travelling in a medium whose relative electric permittivity and relative magnetic permeability bothare 2 . Its velocity in this medium is
$\qquad$ $\times 10^{7} \mathrm{~m} / \mathrm{s}$.
Sol. 15
Given : $\mathrm{f}=5 \mathrm{GHz}$
$\varepsilon_{r}=2$
$\mu_{\mathrm{r}}=2$
velocity of wave $\Rightarrow v=\frac{c}{n}$
where, $\mathrm{n}=\sqrt{\mu_{\mathrm{r}} \varepsilon_{\mathrm{r}}}$ and $\mathrm{c}=$ speed of light $=3 \times 10^{8} \mathrm{~m} / \mathrm{s}$
$\mathrm{n}=\sqrt{2 \times 2}=2$
put the value of $n$ in we get
$\Rightarrow \mathrm{v}=\frac{3 \times 10^{8}}{2}=15 \times 10^{7} \mathrm{~m} / \mathrm{s}$
$\Rightarrow X \times 10^{7}=15 \times 10^{7}$
$X=15$
7. A hydraulic press can lift 100 kg when a mass ' $m$ ' is placed on the smaller piston. It can lift
$\qquad$ kg when the diameter of the larger piston is increased by 4 times and that of the smaller piston is decreased by 4 times keeping the same mass ' $m$ ' on the smaller piston.

## Sol. 25600



Atmospheric pressure $P_{0}$ will be acting on both the limbs of hydraulic lift.
Applying pascal's law for same liquid level
$\Rightarrow P_{0}+\frac{m g}{A_{1}}=P_{0}+\frac{(100) g}{A_{2}}$

$$
\begin{equation*}
\Rightarrow \frac{M g}{A_{1}}=\frac{(100) g}{A_{2}} \Rightarrow \frac{m}{100}=\frac{A_{1}}{A_{2}} \tag{1}
\end{equation*}
$$

Diameter of piston on side of 100 kg is increased by 4 times so new area $=16 \mathrm{~A}_{2}$
Diameter of piston on side of $(\mathrm{m}) \mathrm{kg}$ is decreasing
$A_{1}=\frac{A_{1}}{16}$
(In order to increasing weight lifting capacity, diameter of smaller piston must be reduced)
Again, $\frac{m g}{\left(\frac{A_{1}}{16}\right)}=\frac{M^{\prime} g}{16 A_{2}} \Rightarrow \frac{256 m}{M^{\prime}}=\frac{A_{1}}{A_{2}}$
From equation (1) $=\frac{256 \mathrm{~m}}{M^{\prime}}=\frac{m}{100} \Rightarrow \therefore M^{\prime}=25600 \mathrm{~kg}$
8. A common transistor radio set requires 12 V (D.C.) for its operation. The D.C. source is constructed by using a transformer and a rectifier circuit, which are operated at 220 V (A.C.) on standard domestic A.C. supply. The number of turns of secondary coil are 24 , then the number of turns of primary are $\qquad$ .

## Sol. 440

Given
Primary voltage, $\mathrm{V}_{\mathrm{p}}=220 \mathrm{~V}$
Secondary voltage, $\mathrm{v}_{\mathrm{s}}=12 \mathrm{~V}$
No. of turns in secondary coil is $N_{s}=24$
no. of turns in primary coil, $\mathrm{N}_{\mathrm{p}}=$ ?
We know that for a transformer
$\Rightarrow \frac{\mathrm{N}_{\mathrm{p}}}{\mathrm{N}_{\mathrm{s}}}=\frac{\mathrm{V}_{\mathrm{p}}}{\mathrm{V}_{\mathrm{s}}}$
$\Rightarrow N_{p}=\frac{V_{p} \times N_{s}}{V_{s}}=\frac{220 \times 24}{12}$
$\Rightarrow \mathrm{N}_{\mathrm{p}}=440$
9. An unpolarized light beam is incident on the polarizer of a polarization experiment and the intensity of light beam emerging fromthe analyzer is measured as 100 Lumens. Now, if the analyzer is rotated around the horizontal axis (direction of light) by $30^{\circ}$ in clockwise direction, the intensity of emerging light will be $\qquad$ Lumens.
Sol. 75
Given : $\mathrm{I}_{0}=100$ lumens, $\theta=30^{\circ}$
$\mathrm{I}_{\text {net }}=\mathrm{I}_{0} \cos ^{2} \theta$
$\mathrm{I}_{\text {net }}=100 \times\left(\frac{\sqrt{3}}{2}\right)^{2}=\frac{100 \times 3}{4}$
$\mathrm{I}_{\text {net }}=75$ lumens
10. In connection with the circuit drawn below, the value of current flowing through $2 \mathrm{k} \Omega$ resistor is
$\qquad$ $\times 10^{-4} \mathrm{~A}$.


## Sol. 25

In zener diode there will be o change in current after 5 V zener diode breakdown
$\Rightarrow \mathrm{i}=\frac{5}{2 \times 10^{3}}$
$\Rightarrow i=2.5 \times 10^{-3} \mathrm{~A}$
$\Rightarrow \mathrm{i}=25 \times 10^{-4} \mathrm{~A}$

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