


| LOE (Advanced) |
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## हमारा विश्वास... हर एक विद्यार्यी है खुास

1. Space between two concentric conducting spheres fo radii $a$ and $b(b>a)$ is filled with a medium of ressitivity $\rho$. The resistance between the two spheres will be:
(1) $\frac{\rho}{4 \pi}\left(\frac{1}{a}+\frac{1}{b}\right)$
(2) $\frac{\rho}{4 \pi}\left(\frac{1}{a}-\frac{1}{b}\right)$
(3) $\frac{\rho}{2 \pi}\left(\frac{1}{a}-\frac{1}{b}\right)$
(4) $\frac{\rho}{2 \pi}\left(\frac{1}{a}+\frac{1}{b}\right)$

Sol. 2

$\mathrm{dR}=\mathrm{s} \frac{\mathrm{dr}}{4 \pi \mathrm{r}^{2}}$
$\int d R=\frac{1}{4 \pi} \int_{a}^{b} r^{-2} d r$
$R=\frac{l}{4 \pi}\left[\frac{1}{a}-\frac{1}{b}\right]$
2. A solid spheer of mass $M$ and radius $R$ is divided into two unequal parts. The first part has a mass of $\frac{7 \mathrm{M}}{8}$ and is converted into a uniform disc of radius $2 R$. The second part is converted into a uniform solid sphere. Let $I_{1}$ be the moment of inertia of the disc about its axis and $I_{2}$ be the moment of inertia of the new sphere about its axis. The ratio $I_{1} / I_{2}$ is given by :
(1) 185
(2) 65
(3) 140
(4) 285

Sol. 3
$I_{1}=\frac{1}{4 \pi} \frac{\frac{7 M}{8} 4 R^{2}}{2}=\frac{7 M R^{2} \times 4}{16}$
$I_{1}=\frac{7}{4} M R^{2}$
$I_{2}=\frac{2}{5} \frac{M}{8} R_{1}{ }^{2}=\frac{M R_{1}^{2}}{20}$
$\frac{\mathrm{I}_{1}}{\mathrm{I}_{2}}=\frac{7}{4} \mathrm{MR}^{2} \times$
$=140$
3. A cubical block of side 0.5 m floats on water with $30 \%$ of its volume under water. What is the maximum weight that can be put on the block without fully submerging it under water ?
[Take, density of water $=10^{3} \mathrm{~kg} / \mathrm{m}^{3}$ )
(1) 87.5 kg
(2) 30.1 kg
(3) 65.4 kg
(4) 46.3 kg

## हमारा विश्वास... ही Lक विस्यार्यी है खुास

Sol. 1

$(M+m)=\rho A I$
$m=\rho A I-\frac{3}{10} \rho A I=\frac{7}{10} \rho A I$
$\mathrm{m}=\frac{7 \times 10^{3} \times 0.5 \times 0.5 \times 0.5}{10 \times 1000}$
$\mathrm{m}=87.5 \mathrm{~kg}$
4. A metal coin of mass 5 g and radius 1 cm is fixed to a thin stick $A B$ of negligible mass as shown in the figure. The system is initially at rest. The constant torque, that will make the system rotate about $A B$ at 25 rotations per second in 5 s , is close to -

(1) $1.6 \times 10^{-5} \mathrm{Nm}$
(2) $4.0 \times 10^{-6} \mathrm{Nm}$
(3) $2.0 \times 10^{-5} \mathrm{Nm}$
(4) $7.9 \times 10^{-6} \mathrm{Nm}$

## Sol. 3

$\propto=\frac{2 \pi \times 25}{5}=10 \pi$
$\mathrm{z}=\mathrm{I} \propto=\frac{5}{4} \mathrm{MR}^{2} \times 10 \pi$
$z=\frac{5}{4} \times 5 \times 10^{-3} \times 110^{-4} \times 10 \times 3.14$
$z=\frac{25 \times 3.14}{4} \times 10^{-6} \mathrm{Nm}$
$z=19.6 \times 10^{-6} \approx 2 \times 10^{-5} \mathrm{Nm}$

## हमारा विश्वास... हर एक विद्यार्थी है ख़ास

5. The correct figure that shows, schematically, the wave pattern produced by superposition of two waves of frequencies 9 Hz and 11 Hz , is -
(1)

(2)

(3)

(4)


Sol. 3
$y=A \sin 18 \pi t$
$y=A \sin 11 \pi t$
$\bar{y}=\bar{y}_{1}+\bar{y}_{2}$
$y=A \sin (18 \pi t)+A \sin (11 \pi t)$
$t=0,1,2 y=0$
6. A coil of self inductance 10 mH and resistance $0.1 \Omega$ is connected through a switch to a battery of internal resistance $0.9 \Omega$. After the switch is closed, the time taken for the current to attain $80 \%$ of the saturation value is - [Take $\ln 5=1.6]$
(1) 0.016 s
(2) 0.002 s
(3) 0.103 s
(4) 0.324 s

## Sol. 1

$i=i_{0}\left(1-e^{-\frac{R}{L} t}\right)$
$\frac{8}{10} \mathrm{i}_{0}=\mathrm{i}_{0}\left(1-\mathrm{e}^{-\frac{\mathrm{R}}{\mathrm{L}}}\right)$
$\frac{1}{5}=e^{-\frac{R}{L} t}$
$\operatorname{Ln}(5)=\frac{R}{L} t$
$t=\frac{[x]}{\left[z^{2}\right]} \ln (5)$
$\mathrm{t}=\frac{10 \times 10^{-3}}{\mathrm{l}} \ln (5)$
$\mathrm{t}=10^{-2} \times 1.6$
$t=0.016 \mathrm{sec}$
7. A square loop is carrying a steady curent I and the magnitude of its magnetic dipole moment is m . If this square loop is changed to a circular loop and it carries the same current, the magnitude of the magnetic dipole moment of circular loop will be -
(1) $\frac{4 m}{\pi}$
(2) $\frac{3 m}{\pi}$
(3) $\frac{m}{\pi}$
(4) $\frac{2 m}{\pi}$

## छमारा विश्वास... हु पक विद्यार्यी है खित्य

## Sol. 1


$\mathrm{m}=\mathrm{Ni}^{2}$
$\mathrm{N}=1$
$\mathrm{m}=\mathrm{il}^{2}$

$2 \pi r=41$
$r=\frac{4 l}{2 \pi}=\frac{2 l}{\pi}$
$M=i \pi r^{2}$
$M=i \pi \frac{\left.4\right|^{2}}{\pi^{2}}=\frac{4 m}{\pi}$
8. In the formula $X=5 Y Z^{2}, X$ and $Z$ have dimensions of capacitance and magnetic field, respectively. What are the dimensions of $Y$ in SI units ?
(1) $\left[M^{-2} L^{-2} T^{6} A^{3}\right]$
(2) $\left[M^{-1} L^{-2} T^{4} A^{2}\right]$
(3) $\left[\mathrm{M}^{-2} \mathrm{~L}^{0} \mathrm{~T}^{-4} \mathrm{~A}^{-2}\right]$
(4) $\left[M^{-3} L^{-2} T^{8} A^{4}\right]$

## Sol. 4

$B=M T^{-2} A^{-1}$
$\mathrm{F}=\mathrm{BIL}$
$C=M^{-1} L^{-2} A^{-2} T^{4} C=\frac{q^{2}}{2 E}$
$[y]=\frac{[x]}{\left[z^{2}\right]}=M^{-3} L^{-2} T^{8} A^{+4}$
9. In $\mathrm{Li}^{++}$, electron in first Bohr orbit is excited to a level by a radiation of wavelength $\lambda$. When the ion gets deexcited to the ground state in all possible ways (including intermediate emissions), a total of six spectral lines are observed. What is the value of $\lambda$ ?
[Given : $\mathrm{h}=6.63 \times 10^{-34} \mathrm{Js} ; \mathrm{c}=3 \times 10^{8} \mathrm{~ms}^{-1}$ ] s :
(1) 12.3 nm
(2) 11.4 nm
(3) 10.8 nm
(4) 9.4 nm

Sol. 3
$6=\frac{\mathrm{n}(\mathrm{n}-1)}{2}$
$\mathrm{n}=4=-0.85 \times 9$
$\mathrm{n}=3$
$\mathrm{n}=2$
$\mathrm{n}=1=-13.6 \times 9$
$E=\frac{h c}{\lambda}=\frac{12400}{\lambda \mathrm{~A}^{0}}=114.75$
$\lambda=\frac{12400}{114.75}=108.06 \mathrm{~A}^{0}$
$=10.8 \mathrm{~nm}$

## हमारा विश्वास... हू प्त विद्यार्यी है खुास

10. A source of sound $S$ is moving with a velocity of $50 \mathrm{~m} / \mathrm{s}$ towards a stationary observer. The observer measures the frequency of the source as 1000 Hz . What will be the apparent frequency of the source when it is moving away from the observer after crossing him ? (Take velocity of sound in air is $350 \mathrm{~m} / \mathrm{s}$ )
(1) 857 Hz
(2) 1143 Hz
(3) 750 Hz
(4) 807 Hz

Sol. 3
Source $\quad f^{\prime}=1000 \mathrm{~Hz}$

$f^{\prime}=f\left(\frac{350}{350-50}\right)$
$f^{\prime}=f\left(\frac{350}{350+50}\right)$
$\frac{1000}{f^{\prime}}=\frac{400}{3100}$
$f^{\prime \prime}=\frac{3000}{4}=0.150 \mathrm{~Hz}$
11. Two blocks $A$ and $B$ of masses $m_{A}=1 \mathrm{~kg}$ and $m_{B}=3 \mathrm{~kg}$ are kept on the table as shown in figure. The coefficient of friction between $A$ and $B$ is 0.2 and between $B$ and the surface of the table is also 0.2. The maximum force $F$ that can be applied on $B$ horizontally, so that the block $A$ does not slide over the block $B$ is -
[Take $\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$ ]

(1) 8 N
(2) 16 N
(3) 12 N
(4) 40 N

Sol. 2
$\mathrm{f}_{2 \mathrm{~kg}}=2 \mathrm{~N}$
$a=2 \mathrm{~m} / \mathrm{s}^{2}$
$\mathrm{f}_{3 \mathrm{~kg}}=8 \mathrm{~N}$
$\mathrm{F}^{3 \mathrm{~kg}}-10=3 \times 2$
$\mathrm{F}=16 \mathrm{~N}$
12. The graph shows how the magnification m produced by a thin lens varies with image distance $v$. What is the focal length of the lens used ?

(1) $\frac{b}{c}$
(2) $\frac{b^{2}}{a c}$
(3) $\frac{a}{c}$
(4) $\frac{b^{2} c}{a}$

## हमारा विश्वास... हु पक निद्यार्यी है ख़ास

## Sol. 1

$m=\frac{f-V}{f}=12-\frac{V}{f}$
slope $=-\frac{1}{f}$
$-\frac{1}{f}=\frac{c}{b}$
$f=-\frac{b}{c}$

13. In a Young's double slit experiment, the ratio of the slit's width is 4 : 1. The ratio of the intensity of maxima to minima, close to the central fringe on the screen, will be -
(1) $25: 9$
(2) $(\sqrt{3}+1)^{4}: 16$
(3) $9: 1$
(4) $4: 1$

Sol. 3
$\frac{\mathrm{I}_{1}}{\mathrm{I}_{2}}=\frac{4}{1}$
$\frac{\mathrm{I}_{\text {max }}}{\mathrm{I}_{\text {min }}}=\left(\frac{\sqrt{\mathrm{I}_{1}}+\sqrt{\mathrm{I}_{2}}}{\sqrt{\mathrm{I}_{1}}-\sqrt{\mathrm{I}_{2}}}\right)^{2}$
$\frac{I_{\text {max }}}{\mathrm{I}_{\text {min }}}=\left(\frac{9}{1}\right)$
14. In free space, a particle $A$ of charge $1 \mu C$ is held fixed at a point $P$. Another particle $B$ of the same charge and mass $4 \mu \mathrm{~g}$ is kept at a distance of 1 mm from $P$. If $B$ is released, then its velocity at a distance of 9 mm from $P$ is -
$\left[\right.$ Take $\left.\frac{1}{4 \pi \varepsilon_{0}}=9 \times 10^{9} \mathrm{Nm}^{2} \mathrm{C}^{-2}\right]$
(1) $3.0 \times 10^{4} \mathrm{~m} / \mathrm{s}$
(2) $1.5 \times 10^{2} \mathrm{~m} / \mathrm{s}$
(3) $2.0 \times 10^{3} \mathrm{~m} / \mathrm{s}$
(4) $1.0 \mathrm{~m} / \mathrm{s}$

## Sol. Bonus

$\frac{\mathrm{k} 10^{-6} \times 10^{-6}}{10^{-3}}-\frac{\mathrm{k} 10^{-6} \times 10^{-6}}{9 \times 10^{-3}}=\frac{1}{2} \times 4 \times 10^{-6} \times 10^{-3} \mathrm{v}^{2}$
$\frac{9 \times 10^{9} \times 10^{-6}}{10^{-3}}-\frac{9 \times 10^{9} \times 10^{-6}}{9 \times 10^{-3}}=2 \times 10^{3} \mathrm{v}^{2}$
$9 \times 10^{9} \times 10^{-6}-10^{9} \times 10^{-6}=2 \times 10^{-6} \mathrm{v}^{2}$
$4 \times 10^{9}=v^{2}$
$v=\sqrt{40 \times 10^{8}}$
$v=\sqrt{40} \times 10^{4}$
15. A bullet of mass 20 g has an initial sped of $1 \mathrm{~ms}^{-1}$, just before it starts penetrating a mud wall of thickness 20 cm . If the wall offers a mean resistance of $2.5 \times 10^{-2} \mathrm{~N}$, the speed of the bullet after emerging from the other side of the wall is close to -
(1) $0.3 \mathrm{~ms}^{-1}$
(2) $0.7 \mathrm{~ms}^{-1}$
(3) $0.1 \mathrm{~ms}^{-1}$
(4) $0.4 \mathrm{~ms}^{-1}$

## हमारा विश्वास... हर एक विद्यार्थी है खुखास

Sol. 2
$w=k_{f}-k_{i}$
$-\frac{2 \sqrt{5}}{10} \times 10^{-2} \times \frac{20}{100}=\frac{1}{2} \mathrm{mv}_{\mathrm{f}}{ }^{2}-\frac{1}{2} \mathrm{mv}_{1}^{2}$
$-10^{-2}=m\left(v_{f}^{2}-v_{f}^{2}\right)$
$-\frac{10^{-2}}{20 \times 10^{-3}}=v_{f}^{2}-1$
$v_{f}^{2}=1-\frac{10}{20}=1.5$
$v_{f}=\sqrt{0.5}=0.70 \mathrm{~m} / \mathrm{sec}$
16. When heat $Q$ is supplied to a diatomic gas of rigid molecules, at constant volume its temperature increases by $\Delta T$. The heat required to produce the same change in temperature, at a constant pressure is -
(1) $\frac{5}{3} Q$
(2) $\frac{2}{3} Q$
(3) $\frac{3}{2} Q$
(4) $\frac{7}{5} Q$

Sol. 4
$\mathrm{Q}=\Delta \mathrm{U}$
$Q=\frac{f}{2} n R \Delta T \quad n R \Delta T=\frac{2 Q}{f}$
$Q^{\prime}=w+\frac{f}{2} n R \Delta T$
$Q^{\prime}=n R \Delta T+\frac{f}{2} n R \Delta T$
$Q^{\prime}=n R \Delta T(1+f / 2)$
$Q^{\prime}=\frac{2 Q}{f}(1+f / 2)=\frac{2 Q}{5}(1+5 / 2)$
$\mathrm{Q}^{\prime}=\frac{2 \mathrm{Q}}{5} \cdot \frac{7}{2}=\frac{7}{5} \mathrm{Q}$
17. A submarine experiences a pressure of $5.05 \times 10^{6} \mathrm{~Pa}$ at a depth of $d_{1}$ in a sea. When it goes further to a depth of $d_{2}$, it experiences a pressure of $8.08 \times 10^{6} \mathrm{~Pa}$. Then $d_{2}-d_{1}$ is approximately (density of water $=10^{3} \mathrm{~kg} / \mathrm{m}^{3}$ and acceleration due to gravity $=10 \mathrm{~ms}^{-2}$ )
(1) 600 m
(2) 300 m
(3) 400 m
(4) 500 m

## Sol. 2

$P_{1}=\delta g d_{1}+P_{0}$
$P_{2}^{1}=\delta \mathrm{gd}_{2}+P_{0}^{0}$
$\left(P_{2}-P_{1}\right)=\delta g\left(d_{2}-d_{1}\right)$
$d_{2}-d_{1}=\frac{P_{2}-P_{1}}{\delta g}$
$=\frac{8.08 \times 10^{6}-5.05 \times 10^{6}}{1000 \times 10}$
$=\frac{3.03 \times 10^{6}}{10^{4}}=3.03 \times 10^{2}=300 \mathrm{~m}$
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## हमारा विश्वास... हु पक निद्यार्यी है ख़ास

## MOTION"

18. One mole of an ideal gas passes through a process where pressure and volume obey the relation $P=P_{0}\left[1-\frac{1}{2}\left(\frac{V_{0}}{V}\right)^{2}\right]$. Here $P_{0}$ and $V_{0}$ are constants. Calculate the change in the temperature of the gas if its volume changes from $V_{0}$ to $2 V_{0}$.
(1) $\frac{5}{4} \frac{P_{0} V_{0}}{R}$
(2) $\frac{1}{4} \frac{P_{0} V_{0}}{R}$
(3) $\frac{1}{2} \frac{P_{0} V_{0}}{R}$
(4) $\frac{3}{4} \frac{P_{0} V_{0}}{R}$

## Sol. 1

$P V=n R T$
$\mathrm{T}=\frac{\mathrm{PV}}{\mathrm{nR}} \mathrm{n}=1$ mole
$T=\frac{V}{R}\left[P_{0}\left[1-\frac{1}{2}\left(\frac{V_{0}}{V}\right)^{2}\right]\right]$
$T_{i}=\frac{V_{0}}{R}\left[P_{0}\left[1-\frac{1}{2}\left(\frac{\mathrm{~V}_{0}^{2}}{\mathrm{~V}^{2}}\right)\right]\right]$
$\mathrm{T}_{\mathrm{f}}=\frac{2 \mathrm{~V}_{0}}{\mathrm{R}}\left[\mathrm{P}_{0}\left[1-\frac{1}{2} \frac{\mathrm{~V}_{0}^{2}}{\left(2 \mathrm{~V}_{0}\right)^{2}}\right]\right]$
$T_{i}=\frac{P_{0} V_{0}}{2 R} T_{f}=\frac{7}{4} \frac{P_{0} V_{0}}{R}$
$\therefore \Delta \mathrm{T}=\mathrm{T}_{\mathrm{f}}-\mathrm{T}_{\mathrm{i}}$
$=\frac{7}{4} \frac{P_{0} V_{0}}{R}-\frac{P_{0} V_{0}}{2 R}=\frac{5}{4} \frac{P_{0} V_{0}}{R}$
19. The time dependence of the position of a particle of mass $m=2$ is given by $\vec{r}(t)=2 t \hat{i}-3 t^{2} \hat{j}$. Its angular momentum, with respect to the origin, at time $t=2$ is -
(1) $36 \hat{k}$
(2) $48(\hat{i}+\hat{j})$
(3) $-34(\hat{k}-\hat{i})$
(4) $-48 \hat{k}$

Sol. 4
$L=m(\vec{r} \times \vec{v})$
$r=2 t \hat{i}-3 t^{2} \hat{j}$
at $\mathrm{t}=2$
$\vec{r}=4 \hat{i}-12 \hat{j}$
$\vec{v}=2 \hat{i}-6 t \hat{j}=2 \hat{i}-12 \hat{j}$
$\therefore L=2\left|\begin{array}{ccc}\hat{i} & \hat{j} & \hat{k} \\ 4 & -12 & 0 \\ 2 & -12 & 0\end{array}\right|=-48 \hat{k}$
20. The elastic limit of brass is 379 MPa . What should be the minimum diameter of a brass rod if it is to support a 400 N load without exceeding its elastic limit ?
(1) 1.00 mm
(2) 1.16 mm
(3) 1.36 mm
(4) 0.90 mm

## हमारा विश्वास... हर एक विद्यार्यी है खुास

## Sol. 2

stan $=F / A$
$379 \times 10^{6}=\frac{400}{\pi r^{2}}$
$r=d / 2$
$379 \times 10^{6}=\frac{400}{\pi \times \frac{\mathrm{d}^{2}}{4}}$
$\therefore \mathrm{d}^{2}=\frac{1600}{379 \times 10^{6} \times \pi}$
$d=\sqrt{\frac{1600}{379 \times 10^{6} \times \pi}}$
21. The magnitude of the magnetic field at the center of an equilateral triangular loop of side 1 m which is carrying a current of 10 A is -
[Take $\mu_{0}=4 \pi \times 10^{-7} \mathrm{NA}^{-2}$ ]
(1) $9 \mu \mathrm{~T}$
(2) $18 \mu \mathrm{~T}$
(3) $3 \mu \mathrm{~T}$
(4) $1 \mu \mathrm{~T}$

## Sol. 2


$m$ due to single wine
$B=\frac{\mu_{0}}{4 \pi d_{1}}\left(\sin 60^{\circ}+\sin 60^{\circ}\right)$
$\therefore \mathrm{B}_{\text {net }}=3 \mathrm{~B}_{1}$
$\left(\frac{3 \mu_{0}}{4 \pi \frac{1}{2 \sqrt{3}}}\left(2 \sin 60^{\circ}\right)\right)$
$B=\frac{\mu_{0} i}{4 \pi d}\left(\sin \theta_{1}+\sin \theta_{2}\right)$
$=\frac{\mu_{0} \mathrm{i}(2 \sqrt{3})}{4 \pi \mathrm{I}}\left[2 \sin 60^{\circ}\right]$
$=18 \mu \mathrm{TAm}$
=

## हमारा विश्वास... हर पक निद्यार्थी है ख़ास

22. In an experiment, brass and steel wires of length 1 m each with areas of cross section $1 \mathrm{~mm}^{2}$ are used. The wires are connected in series and one end of the combined wire is connected to a rigid support and other end is subjected to elongation. The stress required to produce a net elongation of 0.2 mm is,
[Given, the Young's Modulus for steel and brass are, respectively, $120 \times 10^{9} \mathrm{~N} / \mathrm{m}^{2}$ and $60 \times 10^{9} \mathrm{~N} / \mathrm{m}^{2}$ ]
(1) $4.0 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
(2) $1.2 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
(3) $0.2 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
(4) $1.8 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$

## Sol. Bonus

$y_{w}=\frac{\text { stream }}{\left(\frac{\mathrm{OI}}{\mathrm{loop}}\right)}$
$\frac{2 l}{y_{w} A}=\frac{1}{y_{1} A}+\frac{1}{y_{2} A}$
$y_{w}=\frac{2 y_{1} y_{2}}{\left(y_{1}+y_{2}\right)}$
steam $=y_{w} \times \frac{\Delta I}{\left(l_{1}+I_{2}\right)}$
$=8 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
23. A spaceship orbits around a planet at a height of 20 km from its surface. Assuming that only gravitational field of the planet acts on the spaceship, what will be the number of complete revolutions made by the spaceship in 24 hours around the planet ?
[Given : mass of planet $=8 \times 10^{22} \mathrm{~kg}$, Radius of planet $=2 \times 10^{6} \mathrm{~m}$, Gravitational constant $\mathrm{G}=$ $\left.6.67 \times 10^{-11} \mathrm{Nm}^{2} / \mathrm{kg}^{2}\right]$
(1) 9
(2) 17
(3) 11
(4) 13

## Sol. 3

$T=2 \pi \sqrt{\frac{\left(R_{e}+h\right)^{3}}{6 m}}$
$T=2 \pi\left(\frac{\left(2 \times 10^{6}+2000\right)^{3}}{G \times M}\right)$
24. A plane is inclined at an angle $\alpha=30^{\circ}$ with respect to the horizontal. A particle is projected with a speed $u=2 \mathrm{~ms}^{-1}$, from the base of the plane, making an angle $\theta=15^{\circ}$ with respect to the plane as shown in the figure. The distance from the base, at which the particle hits the plane is close to
(Take $\mathrm{g}=10 \mathrm{~ms}^{-2}$ )

(1) 18 cm
(2) 20 cm
(3) 14 cm
(4) 26 cm

## Sol. 2.

$R=\frac{2 \mathrm{u}^{2} \sin \alpha \cos (\alpha+\beta)}{\mathrm{g} \cos ^{2} \beta}$
$\alpha=15^{\circ}$
$\beta=30^{\circ}$
$\mathrm{u}=2 \mathrm{~m} / \mathrm{s}$

## हमारा विश्वास... हर एक विद्यार्यी है ख़ास

25. Water from a tap emerges vertically downwards with an initial speed of $1.0 \mathrm{~ms}^{-1}$. The crosssectional area of tap is $10^{-4} \mathrm{~m}^{2}$. Assume that the pressure is constant throughout the stream of water and that the flow is streamlined. The cross-sectional area of the stream, 0.15 m below the tap would be -
[Take $\mathrm{g}=10 \mathrm{~ms}^{-2}$ ]
(1) $1 \times 10^{-5} \mathrm{~m}^{2}$
(2) $5 \times 10^{-5} \mathrm{~m}^{2}$
(3) $5 \times 10^{-4} \mathrm{~m}^{2}$
(4) $2 \times 10^{-5} \mathrm{~m}^{2}$

Sol. 2

$A_{1} v_{1}=A_{2} v_{2}$
$1 \times 10^{-4}=A_{2} \times \sqrt{1^{2}+2 \times g \times 0.15}$
$1 \times 10^{-4}=A_{2} \times 2$
26. A 2 mW laser operates at a wavelength of 500 nm . The number of photons that will be emitted per second is -
[Given Planck's constant $\mathrm{h}=6.6 \times 10^{-34} \mathrm{Js}$, speed of light $\mathrm{c}=3.0 \times 10^{8} \mathrm{~m} / \mathrm{s}$ )
(1) $5 \times 10^{15}$
(2) $2 \times 10^{16}$
(3) $1.5 \times 10^{16}$
(4) $1 \times 10^{16}$

Sol. 1
$\mathrm{P}=2 \mathrm{nw} \quad \lambda=500 \mathrm{~nm}$
$\mathrm{n}=\frac{\mathrm{IAt} \lambda}{\mathrm{hc}}$
$=\frac{10^{-9} \times 10^{34} \times 10^{-8}}{19.8}=\frac{10^{17}}{19.8}$
27. The figure represents a voltage regulator circuit using a Zener diode. The breakdown voltage of the Zener diode is 6 V and the load ressitance is, $R_{L}=4 \mathrm{k} \Omega$. The series resistance of the circuit is $\mathrm{R}_{\mathrm{i}}=1 \mathrm{k} \Omega$. If the battery voltage $\mathrm{V}_{\mathrm{B}}$ varies from 8 V to 16 V , what are the minimum and maximum values of the current through Zener diode ?

(1) 0.5 mA ; 6 mA
(2) $1 \mathrm{~mA} ; 8.5 \mathrm{~mA}$
(3) $1.5 \mathrm{~mA} ; 8.5 \mathrm{~mA}$
(4) $0.5 \mathrm{~mA} ; 8.5 \mathrm{~mA}$

Fee ₹ 1500

## हमारा विश्वास... हर एक विद्यार्यी है खुास

Sol. 4
$\mathrm{V}_{2}=6$ volt
$\mathrm{V}_{0}=8$ volt

$i=\frac{8-6}{1000}=\frac{2}{1000}=2 \mathrm{ma}$
$i_{2}=\frac{6}{4000}=1.5 \mathrm{~mA}$
$\mathrm{i}=\mathrm{i}_{\mathrm{z}}+\mathrm{i}_{2}$
$\mathrm{i}_{\mathrm{z}}=\mathrm{i}-\mathrm{i}_{2}$
$=2-15$
$=0.5 \mathrm{~mA}$

$i=\frac{16-6}{10^{3}}=10 \mathrm{~mA}$
$\mathrm{i}_{2}=1.5 \mathrm{~mA}$
$i_{2}=10-1.56$
$=8.5 \mathrm{~mA}$
28. Two radioactive substances $A$ and $B$ have decay constants $5 \lambda$ and $\lambda$ respectively. At $t=0, a$ sample has the same number of teh two nuclei. The time taken for the ratio of the number of nuclei to become $\left(\frac{1}{e}\right)^{2}$ will be -
(1) $1 / \lambda$
(2) $1 / 4 \lambda$
(3) $1 / 2 \lambda$
(4) $2 / \lambda$

Sol. 3
$N_{1}=N_{0} e^{-5 \lambda t}$
$N_{2}=N_{0} e^{-\lambda t}$
$\frac{N_{1}}{N_{2}}=\frac{e^{-5 \lambda t}}{e^{-\lambda t}}$
$\left(\frac{1}{\mathrm{e}}\right)^{2}=\frac{1}{\mathrm{e}^{+4 \lambda t}}$
on solving we get
$\mathrm{t}=\frac{1}{2 \lambda}$

## हमारा विश्वास... हा एक विद्यार्यी है खुास

29. A simple pendulum of length $L$ is placed between the plates of a parallel plate capacitor having electric field $E$, as shown in figure. Its bob has mass $m$ and charge $q$. The time period of the pendulum is given by -

(1) $2 \pi \sqrt{\frac{L}{\sqrt{g^{2}+\left(\frac{q E}{m}\right)^{2}}}}$
(2) $2 \pi \sqrt{\frac{L}{\left(g-\frac{q E}{m}\right)}}$
(3) $2 \pi \sqrt{\frac{L}{\left(g+\frac{q E}{m}\right)}}$
(4) $2 \pi \sqrt{\frac{L}{\sqrt{g^{2}-\frac{q^{2} E^{2}}{m^{2}}}}}$

## Sol. 1

$g_{\text {eff }}=\sqrt{g^{2}+\left(\frac{q E}{m}\right)^{2}}$
$\therefore T=2 \pi \sqrt{\frac{1}{\sqrt{g^{2}+\left(\frac{q E}{m}\right)^{2}}}}$
30. Light is incident normally on a completely absorbing surface with an energy flux of $25 \mathrm{Wcm}^{-2}$. If the surface has an area of $25 \mathrm{~cm}^{2}$, the momentum transferred to the surface in 40 min time duration will be -
(1) $3.5 \times 10^{-6} \mathrm{Ns}$
(2) $6.3 \times 10^{-4} \mathrm{Ns}$
(3) $5.0 \times 10^{-3} \mathrm{Ns}$
(4) $1.4 \times 10^{-6} \mathrm{Ns}$

Sol. 3
For Absorption
$F=\frac{I A}{C}$
$\frac{\Delta \mathrm{P}}{\Delta \mathrm{T}}=\frac{\mathrm{IA}}{\mathrm{C}}$
$\Delta P=\frac{I A \times \Delta t}{C}$
$\Delta \mathrm{p}=\frac{25 \times 25 \times 40 \times 60}{3 \times 10^{8}}$
$=5.0 \times 10^{-3} \mathrm{NS}$

## मोशन ने बनाया साधारण को असाधारण JEE Main Result Jan'19 4 RESIDENTIAL COACHING PROGRAM (DRONA) STUDENTS ABOVE 99.9 PERCENTILE



Total Students Above 99.9 percentile - 17
Total Students Above 99 percentile - 282
Total Students Above 95 percentile - 983


Scholarship on the Basis of 12th Class Result

| Marks <br> PCM or PCB | Hindi State <br> Board | State Eng <br> OR CBSE |
| :--- | :---: | :---: |
| $\mathbf{7 0 \% - 7 4 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{2 0 \%}$ |
| $\mathbf{7 5 \% - 7 9 \%}$ | $\mathbf{3 5 \%}$ | $\mathbf{2 5 \%}$ |
| $\mathbf{8 0 \% - 8 4 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{3 5 \%}$ |
| $\mathbf{8 5 \% - 8 7 \%}$ | $\mathbf{5 0 \%}$ | $\mathbf{4 0 \%}$ |
| $\mathbf{8 8 \% - 9 0 \%}$ | $\mathbf{6 0 \%}$ | $\mathbf{5 5 \%}$ |
| $\mathbf{9 1 \% - 9 2 \%}$ | $\mathbf{7 0 \%}$ | $\mathbf{6 5 \%}$ |
| $\mathbf{9 3 \% - 9 4 \%}$ | $\mathbf{8 0 \%}$ | $\mathbf{7 5 \%}$ |
| $\mathbf{9 5 \%}$ \& Above | $\mathbf{9 0 \%}$ | $\mathbf{8 5 \%}$ |

New Batches for Class $11^{\text {th }}$ to $12^{\text {th }}$ pass 17 April 2019 \& 01 May 2019

हिन्दी माध्यम ते लिए पृयक्तैत

Scholarship on the Basis of JEE Main Percentile

