


Motion
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## हमारा विश्वास... हर एक विद्यार्थी है खुखास

1. A ball is thrown upward with an initial velocity $V_{0}$ from the surface of the earth. The motion of the ball is affected by a drag force equal to $m \gamma v^{2}$ (where $m$ is mass of the ball, $v$ is its instantaneous velocity and $\gamma$ is a constant). Time taken by the ball to rise to its zenith is :
(1) $\frac{1}{\sqrt{2 \gamma g}} \tan ^{-1}\left(\sqrt{\frac{2 \gamma}{g}} V_{0}\right)$
(2) $\frac{1}{\sqrt{\gamma g}} \operatorname{In}\left(1+\sqrt{\frac{\gamma}{g}} V_{0}\right)$
(3) $\frac{1}{\sqrt{\gamma g}} \sin ^{-1}\left(\sqrt{\frac{\gamma}{g}} V_{0}\right)$
(4) $\frac{1}{\sqrt{\gamma g}} \tan ^{-1}\left(\sqrt{\frac{\gamma}{g}} \mathrm{~V}_{0}\right)$

Sol. 4
$\frac{m d u}{d t}=-\left(m g+m \gamma u^{2}\right)$
$\frac{d u}{d t}=-\left(g+\gamma u^{2}\right)$
$\int_{v_{0}} \frac{d u}{\left(g+\gamma u^{2}\right)}=\int_{0}^{t}-d t$
$\therefore \mathrm{t}=\frac{1}{\sqrt{\gamma g}} \tan ^{-1}\left(\sqrt{\frac{\gamma}{g}} \mathrm{v}_{0}\right)$
2. Two radioactive materials $A$ and $B$ have decay constants $10 \lambda$ and $\lambda$, respectively. If initially they have the same number of nuclei, then the ratio of the number of nuclei of $A$ to that of $B$ will be 1/e after a time :
(1) $\frac{11}{10 \lambda}$
(2) $\frac{1}{10 \lambda}$
(3) $\frac{1}{9 \lambda}$
(4) $\frac{1}{11 \lambda}$

Sol. 3
Decay at $\mathrm{t}=0$

| $A$ | $B$ |
| :--- | :--- |
| $10 \lambda$ | $\lambda$ |
| $N_{0}$ | $N_{0}$ |
| $N_{A}=N_{0} e^{-10 \lambda t}$ |  |
| and |  |
| $N_{B}=N_{0} e^{-\lambda t}$ |  |
| $\frac{N_{A}}{N_{B}}=\frac{e^{-10 \lambda t}}{e^{-\lambda t}}$ |  |
| $\frac{N_{A}}{N_{B}}=e^{-9 \lambda t}=\frac{1}{e}$ |  |
| $\Rightarrow 9 \lambda t=1$ |  |
| $\therefore t=\frac{1}{9 \lambda}$ |  |

3. A cylinder with fixed capacity of 67.2 lit contains helium gas at STP. The amount of heat needed to raise the temperature of the gas by $20^{\circ} \mathrm{C}$ is : [Given that $\mathrm{R}=8.31 \mathrm{~J} \mathrm{~mol}^{-1} \mathrm{~K}^{-1}$ ]
(1) 700 J
(2) 350 J
(3) 748 J
(4) 374 J

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Sol. 3
$Q=n C_{v} \Delta T=\frac{67.2}{22.4}\left(\frac{3}{2} R\right)(20$
$=748 \mathrm{~J}$
4. An npn transistor operates as a common emitter amplifier, with a power gain of 60 dB . The input circuit resistance is $100 \Omega$ and the output load resistance is $10 \mathrm{k} \Omega$. The common emitter current gain $\beta$ is :
(1) $10^{4}$
(2) $10^{2}$
(3) $6 \times 10^{2}$
(4) 60

Sol. 2
powe gain $=\beta^{2} \frac{R_{0}}{R_{L}}$
5. A ray of light AO in vacuum is incident on a glass slab at angle $60^{\circ}$ and refracted at angle $30^{\circ}$ along $O B$ as shown in the figure. The optical path length of light ray from $A$ to $B$ is :

(1) $2 a+\frac{2 b}{3}$
(2) $\frac{2 \sqrt{3}}{a}+2 b$
(3) $2 a+\frac{2 b}{\sqrt{3}}$
(4) $2 a+2 b$

## Sol. 4


$A O=\frac{a}{\cos 60^{\circ}}=2 a$
$\mathrm{OB}=\frac{\mathrm{b}}{\cos 30^{\circ}}=\frac{2 \mathrm{~b}}{\sqrt{3}}$
Optical path length
$=A O+\mu O B$
$=2 a+\sqrt{3} \cdot \frac{2 b}{\sqrt{3}}$
$=2(a+b)$

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6. Two coaxial discs, having moments of inertia $I_{1}$ and $\frac{I_{1}}{2}$, are rotating with respective angular velocities $\omega_{1}$ and $\frac{\omega_{1}}{2}$, about their common axis. They are brought in contact $X$ with each other and thereafter they rotate with a common angular velocity. If $E_{f}$ and $E_{i}$ are the final and initial total energies, then $\left(E_{f}-E_{i}\right)$ is :
(1) $\frac{I_{1} \omega_{1}^{2}}{6}$
(2) $-\frac{I_{1} \omega_{1}^{2}}{24}$
(3) $\frac{3}{8} I_{1} \omega_{1}^{2}$
(4) $-\frac{I_{1} \omega_{1}^{2}}{12}$

## Sol. 2

$\omega=\frac{\mathrm{I}_{1} \omega_{1}+\frac{\mathrm{I}_{1}}{2} \cdot \frac{\omega_{1}}{2}}{\mathrm{I}_{1}+\mathrm{I}_{1} / 2}=\frac{\frac{5}{4} \mathrm{I}_{1} \omega_{1}}{\frac{3}{2} \mathrm{I}_{1}}=\frac{5}{6} \omega_{1}$
Loss of energy $=E_{f}-E_{i}$
$=\frac{1}{2} I_{1} W_{1}{ }^{2}+\frac{1}{2}\left(\frac{I_{1}}{2} \frac{W_{1}^{2}}{4}\right)-\frac{1}{2}\left(\frac{3}{2} I_{1}\right)\left(\frac{5}{6} W_{1}^{2}\right)^{2}$
$=\frac{9}{16} \mathrm{I}_{1} \omega_{1}{ }^{2}-\frac{75}{144} \mathrm{I}_{1} \omega_{1}{ }^{2}$
$=\frac{81-75}{144} \mathrm{I}_{1} \omega_{1}{ }^{2}=\frac{6 \mathrm{I}_{1} \omega_{1}^{2}}{144}=\frac{\mathrm{I}_{1} \omega_{1}^{2}}{24}$
$\Delta \mathrm{E}=-\mathrm{I}_{1} \mathrm{~W}_{1}{ }^{2} / 24$
7. Two particles, of masses $M$ and $2 M$, moving, as shown, with speeds of $10 \mathrm{~m} / \mathrm{s}$ and $5 \mathrm{~m} / \mathrm{s}$, collide elastically at the origin. After the collision, they move along the indicated directions with speeds $v_{1}$ and $v_{2}$, respectively. They values of $v_{1}$ and $v_{2}$ are nearly:

(1) $6.5 \mathrm{~m} / \mathrm{s}$ and $3.2 \mathrm{~m} / \mathrm{s}$
(2) $3.2 \mathrm{~m} / \mathrm{s}$ and $6.3 \mathrm{~m} / \mathrm{s}$
(3) $3.2 \mathrm{~m} / \mathrm{s}$ and $12.6 \mathrm{~m} / \mathrm{s}$
(4) $6.5 \mathrm{~m} / \mathrm{s}$ and $6.3 \mathrm{~m} / \mathrm{s}$

## Sol. 4

From momentum conservation


## हमारा विश्वास... हर एक विद्यार्थी है खुखास

Along : $x 10 \mathrm{M} \cos 30^{\circ}+10 \mathrm{M} \cos 45^{\circ}=2 \mathrm{MV}_{1} \cos 30^{\circ}+\mathrm{MV}_{2} \cos 45^{\circ}$
Along : y $-10 \mathrm{M} \sin 30^{\circ}+10 \mathrm{M} \cos 45^{\circ}=2 M V_{1} \sin 30^{\circ}-M V_{2} \cos 45^{\circ}$
Solving we get $\quad \begin{aligned} & \mathrm{V}_{1}=6.31 \mathrm{~m} / \mathrm{s} \\ & \mathrm{V}_{2}=11.16 \mathrm{~m} / \mathrm{s}\end{aligned}$
8. A current of 5 A passes through a copper conductor (resistivity $=1.7 \times 10^{-8} \Omega \mathrm{M}$ ) of radius of crosssection 5 mm . Find the mobility of the charges if their drift velocity is $1.1 \times 10^{-3} \mathrm{~m} / \mathrm{s}$.
(1) $1.5 \mathrm{~m}^{2} / \mathrm{Vs}$
(2) $1.3 \mathrm{~m}^{2} / \mathrm{Vs}$
(3) $1.0 \mathrm{~m}^{2} / \mathrm{Vs}$
(4) $1.8 \mathrm{~m}^{2} / \mathrm{Vs}$

Sol. 3
$\mathrm{V}_{\mathrm{d}}=\mu \mathrm{E}=\mu \frac{\mathrm{V}}{\mathrm{l}}=\frac{\mu}{\mathrm{l}} \mathrm{iR}=\frac{\mu \mathrm{i}}{\mathrm{l}} \cdot \frac{\delta \mathrm{l}}{\mathrm{A}}=\frac{\mu \mathrm{il}}{\mathrm{A}}$
$\therefore \mu=\frac{\mathrm{V}_{\mathrm{d}} \mathrm{A}}{\mathrm{i} \delta}=1.57 \mathrm{~m}^{2} / \mathrm{vs}$
9. In the given circuit, an ideal voltmeter connected across the $10 \Omega$ resistance reads 2 V . The internal resistance $r$, of each cell is :

(1) $1 \Omega$
(2) $0.5 \Omega$
(3) $1.5 \Omega$
(4) $0 \Omega$

Sol. 2

$I_{1}=\frac{1}{7.5}+\frac{1}{5}=\frac{1+1.5}{7.5}$
$(8+2 r) \frac{1}{3}=3$
$\therefore 8+2 r=9$
$r=1 / 2=0.5 \Omega$
10. A particle of mass $m$ is moving along a trajectory given by
$x=x_{0}+a \cos \omega_{1} t$
$y=y_{0}+b \sin \omega_{2} t$
The torque, acting on the particle about the origin, at $t=0$ is :
(1) $+\mathrm{my}_{0} \mathrm{a} \omega_{1}^{2} \hat{\mathrm{k}}$
(2) $m\left(-x_{0} b+y_{0} a\right) \omega_{1}^{2} \hat{k}$
(3) Zero
(4) $m\left(x_{0} b \omega_{2}^{2}-y_{0} a \omega_{1}^{2} \hat{k}\right) \hat{k}$

## हमारा विश्वास... हर एक विद्यार्यी है ख़ास

Sol. 1

$$
\begin{array}{ll}
\text { at } t=0 & x=x_{0}+a \\
& y=y_{0}=0
\end{array}
$$

$v=\frac{d x}{d t} \hat{i}+\frac{d y}{d t} \hat{j}$
$a=\frac{d^{2} x}{d t^{2}} \hat{i}+\frac{d^{2} y}{d t^{2}} \hat{j}$
$\vec{\tau}=\vec{r} \times \vec{F}$
$\vec{\tau}=m(\vec{r} \times \vec{a})$
$\vec{\tau}=m\left(\left(x_{0}+a\right) \hat{i}+y_{0} \hat{j}\right] \times\left[\frac{d^{2} x}{d t^{2}} \hat{i}+\frac{d^{2} y}{d t^{2}} \hat{j}\right]$
$\vec{\tau}=\mathrm{my}_{0} \mathrm{aw}_{1}{ }^{2} \hat{\mathrm{k}}$
11. Given below in the left column are different modes of communication using the kinds of waves given in the right column.
A. Optical Fibre Communication
P. Ultrasound
B. Radar
Q. Infrared Light
C. Sonar
R. Microwaves
D. Mobile Phones
S. Radio Waves

From the options given below, find the most appropriate match between entries in the left and the right column.
(1) $A-Q, B-S, C-R, D-P$
(2) $A-R, B-P, C-S, D-Q$
(3) $A-Q, B-S, C-P, D-R$
(4) $A-S, B-Q, C-R, D-P$

Sol. 3
$A \rightarrow S$
$B \rightarrow R$
$C \rightarrow P$
$\mathrm{D} \rightarrow \mathrm{Q}$
12. $n$ moles of an ideal gas with constant volume heat capacity $C_{v}$ undergo an isobaric expansion by certain volume. The ratio of the work done in the process, to the heat supplied is :
(1) $\frac{4 n R}{C_{v}+n R}$
(2) $\frac{n R}{C_{v}+n R}$
(3) $\frac{4 n R}{C_{v}-n R}$
(4) $\frac{n R}{C_{v}-n R}$

Sol. 2
$\Delta \mathrm{w}=\mathrm{nR} \Delta \mathrm{T}$
$\Delta \mathrm{Q}=\Delta \mathrm{W}+\Delta \mathrm{U}$
$=n R \Delta T+n\left(\frac{C_{v}}{n}\right) \Delta T$
$=\left(n R+C_{v}\right) \Delta T$
$\therefore \frac{\Delta \mathrm{w}}{\Delta \mathrm{Q}}=\frac{\mathrm{nR} \Delta \mathrm{T}}{\left(\mathrm{nR}+\mathrm{C}_{\mathrm{v}}\right) \Delta \mathrm{T}}=\left(\frac{\mathrm{nR}}{\mathrm{nR}+\mathrm{C}_{\mathrm{v}}}\right)$
13. A transformer consisting of 300 turns in the primary and 150 turns in the secondary gives output power of 2.2 kW . If the current in the secondary coil is 10 A , then the input voltage and current in the primary coil are :
(1) 220 V and 10 A
(2) 440 V and 20 A
(3) 220 V and 20 A
(4) 440 V and 5 A

## हमारा विश्वास... हर एक विद्यार्यी है खुास

## Sol. 4

$\mathrm{n}_{\mathrm{p}}: \mathrm{n}_{\mathrm{s}}=2: 1$
$P_{0}=2.2 \mathrm{~kW}$
$\mathrm{i}_{0}=10 \mathrm{~A}$
$\mathrm{V}_{0}=\frac{P_{0}}{i_{0}}=\frac{2.2 \times 10^{3}}{10}=220 \mathrm{~V}$
$\therefore \mathrm{V}_{\mathrm{i}}-2 \times 220 \mathrm{~V}$
$=440 \mathrm{~V}$
and $i_{i}=\frac{P_{i}}{V_{i}}=\frac{2.2 \times 10^{3}}{440}=5 \mathrm{~A}$
14. In an experiment, the resistance of a material is plotted as a function of temperature (in some range). As shown in the figure, it is a straight line.


One may conclude that :
(1) $R(T)=R_{0} e^{-T^{2} / T_{0}{ }^{2}}$
(2) $R(T)=\frac{R_{0}}{T^{2}}$
(3) $R(T)=R_{0} e^{-T_{0}^{2} / T^{2}}$
(4) $R(T)=R_{0} e^{T^{2} / T_{0}^{2}}$

## Sol. 3

$y=m x+C$
$\ln R=-m \frac{1}{T^{2}}+C$
$R=e^{-m / T^{2}}\left(e^{c}\right)$
$R=R_{0} e^{-m / T^{2}}$
15. In a meter bridge experiment, the circuit diagram and the corresponding observation table are shown in figure.


| SI. No. | $R(\Omega)$ | $\ell(\mathrm{cm})$ |
| :--- | :--- | :--- |
| 1. | 1000 | 60 |
| 2. | 100 | 13 |
| 3. | 10 | 1.5 |
| 4. | 1 | 1.0 |

Which of the readings is inconsistent ?
(1) 2
(2) 3
(3) 4
(4) 1

## हमारा विश्वास... ही पक विस्यार्थी है खुास

Sol. 3
$\frac{x}{R}=\left(\frac{100-1}{l}\right)$
$X=R \frac{(100-I)}{I}$
16. A message signal of frequency 100 MHz and peak voltage 100 V is used to execute amplitude modulation on a carrier wave of frequency 300 GHz and peak voltage 400 V . The modulation index and difference between the two side band frequencies are :
(1) $0.25 ; 1 \times 10^{8} \mathrm{~Hz}$
(2) $0.25 ; 2 \times 10^{8} \mathrm{~Hz}$
(3) $4 ; 1 \times 10^{8} \mathrm{~Hz}$
(4) 4 ; $2 \times 10^{8} \mathrm{~Hz}$

## Sol. 2

$$
\left\{\begin{array}{l}
f_{\mathrm{m}}=100 \mathrm{~Hz} \text { (message) } \\
\mathrm{V}_{0}=1000 \text { (peak) }
\end{array}\right.
$$

$\left\{\begin{array}{l}\mathrm{f}_{\mathrm{C}}=300 \mathrm{GHz} \\ \mathrm{V}_{\mathrm{o}}=400 \mathrm{~V} \text { (peak) carrier }\end{array}\right.$
Modulation index $=\frac{\left(V_{0}\right)_{\text {message }}}{\left(V_{0}\right)_{c}}=\frac{100}{400}=\frac{1}{4}$
$f_{\text {max }}-f_{\text {min }}=\left(f_{c}+f_{m}\right)-\left(f_{c}-f_{m}\right)$
$=2 \mathrm{f}_{\mathrm{m}}=2 \times 10^{8} \mathrm{~Hz}$
17. A thin disc of mass $M$ and radius $R$ has mass per unit area $\sigma(r)=k r^{2}$ where $r$ is the distance from its centre. Its moment of inertia about an axis going thought its centre of mass and perpendicular to its plane is :
(1) $\frac{2 M R^{2}}{3}$
(2) $\frac{M R^{2}}{3}$
(3) $\frac{M R^{2}}{6}$
(4) $\frac{M R^{2}}{2}$

## Sol. 1

$\mathrm{dm}=(\mathrm{dA})(\sigma)$
$\mathrm{dm}=(2 \pi \mathrm{rdr})\left(\mathrm{kr}{ }^{2}\right)$
$\mathrm{dI}=\mathrm{dm}-\mathrm{r}^{2}=2 \pi \mathrm{kr} \mathrm{r}^{3} \mathrm{dr} . \mathrm{r}^{2}$
$d I=2 \pi k r^{5} d r$
$I=2 \pi k \cdot \frac{r^{6}}{6}$
and $m=2 \pi k \int_{u}^{r} r^{3} d r=2 \pi k \frac{r^{4}}{4}$

$\frac{\mathrm{I}}{\mathrm{m}}=\frac{2 \pi \mathrm{kr}^{6}}{6} \times \frac{4}{2 \pi \mathrm{kr}^{4}}=\frac{2 \mathrm{r}^{2}}{3}$
$I=\frac{2 m r^{2}}{3}$

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18. The electric field of a plane electromagnetic wave is given by $\overrightarrow{\mathrm{E}}=\mathrm{E}_{0} \hat{i} \cos (\mathrm{kz}) \cos (\omega \mathrm{t})$
The corresponding magnetic field $\vec{B}$ is then given by :
(1) $\vec{B}=\frac{E_{0}}{C} \hat{k} \sin (k z) \cos (\omega t)$
(2) $\vec{B}=\frac{E_{0}}{C} \hat{j} \cos (k z) \sin (\omega t)$
(3) $\vec{B}=\frac{E_{0}}{C} \hat{j} \sin (k z) \cos (\omega t)$
(4) $\vec{B}=\frac{E_{0}}{C} \hat{j} \sin (k z) \sin (\omega t)$

## Sol. 4

19. The value of acceleration due to gravity at Earth's surface is $9.8 \mathrm{~ms}^{-2}$. The altitude above its surface at which the accelerate due to gravity decreases to $4.9 \mathrm{~ms}^{-2}$, is close to : (Radius of earth $=6.4 \times 10^{6} \mathrm{~m}$ )
(1) $9.0 \times 10^{6} \mathrm{~m}$
(2) $1.6 \times 10^{6} \mathrm{~m}$
(3) $6.4 \times 10^{6} \mathrm{~m}$
(4) $2.6 \times 10^{6} \mathrm{~m}$

## Sol. 4

$g_{n}=g .\left(1+\frac{h}{R}\right)^{-2}$
$\frac{g}{2}=g\left(1+\frac{h}{R}\right)^{-2}$
$\left(1+\frac{h}{R}\right)=\sqrt{2}$
$h=(\sqrt{2}-1) R$
$h=2.6 \times 10^{6} \mathrm{~m}$
20. The ratio of surface tensions of mercury and water is given to be 7.5 while the ratio of their densities is 13.6. Their contact angles, with glass, are close to $135^{\circ}$ and $0^{\circ}$, respectively, It is observed that mercury gets depressed by an amount $h$ in a capillary tube or radius $r_{1}$, while water rises by the same amount $h$ in a capillary tube of radius $r_{2}$. The ratio, $\left(r_{1} / r_{2}\right)$, is then close to :
(1) $3 / 5$
(2) $2 / 5$
(3) $4 / 5$
(4) $2 / 3$

Sol. 2

$$
\begin{array}{ll}
\frac{\mathrm{T}_{\mathrm{Hg}}}{\mathrm{~T}_{\mathrm{w}}}=7.5 & \frac{\delta_{\mathrm{hg}}}{\delta_{\omega}}=13.6 \\
\theta_{\mathrm{Hg}}=135^{\circ} & \text { and } \theta_{\text {glass }}=0^{\circ} \\
\mathrm{h}=\frac{27 \cos \theta}{\mathrm{r} \delta \mathrm{~g}} & \\
\frac{\mathrm{r}_{\mathrm{Hg}}}{\mathrm{r}_{\omega}}=\frac{\mathrm{T}_{\mathrm{Hg}}}{\mathrm{~T}_{\omega}} \cdot \frac{\cos \theta_{\mathrm{Hg}}}{\cos \theta_{\mathrm{w}}} \cdot \frac{\delta_{\mathrm{w}}}{\delta_{\mathrm{hg}}} \\
=(7.5)\left(\frac{1 / \sqrt{2}}{1}\right) \frac{1}{13.6} \\
=\frac{7.5}{(\sqrt{2})(13.6)}=0.4=\frac{2}{5}
\end{array}
$$

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21. Figure shows charge ( $q$ ) versus voltage $(\mathrm{V})$ graph for series and parallel combination of two given capacitors, The capacitances are :

(1) $50 \mu \mathrm{~F}$ and $30 \mu \mathrm{~F}$
(2) $60 \mu \mathrm{~F}$ and $40 \mu \mathrm{~F}$
(3) $40 \mu \mathrm{~F}$ and $10 \mu \mathrm{~F}$
(4) $20 \mu \mathrm{~F}$ and $30 \mu \mathrm{~F}$

## Sol. 3

in series

$\frac{\mathrm{C}_{1} \mathrm{C}_{2}}{\mathrm{C}_{1}+\mathrm{C}_{2}}=\frac{500}{10}=50$
In parallel

$C_{1}+C_{2}=\frac{80}{10}=8$
$\therefore \mathrm{C}_{1} \mathrm{C}_{2}=400$
22. In a photoelectric effect experiment the threshold wavelength of light is 380 nm . If the wavelength of incident light is 260 nm , the maximum kinetic energy of emitted electrons will be :

Given $E($ in eV$)=\frac{1237}{\lambda(\text { in } \mathrm{nm})}$
(1) 1.5 eV
(2) 4.5 eV
(3) 3.0 eV
(4) 15.1 eV

Sol. 1
$E_{p}=\frac{1237}{260} \mathrm{ev}=4.75 \mathrm{ev}$
$Q=\frac{1237}{300} \mathrm{ev}=3.25 \mathrm{ev}$
$\mathrm{K}_{\max }=\mathrm{E}-\mathrm{Q}=1.5 \mathrm{ev}$
Fee ₹ 1500

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23. One plano-convex and one plano-concave lens of same radius of curvature ' $R$ ' but of different materials are joined side by side as shown in the figure. If the refractive index of the material of 1 is $\mu_{1}$ and that of 2 is $\mu_{2}$, then the focal length of the combination is:

(1) $\frac{\mathrm{R}}{2\left(\mu_{1}-\mu_{2}\right)}$
(2) $\frac{\mathrm{R}}{2-\left(\mu_{1}-\mu_{2}\right)}$
(3) $\frac{\mathrm{R}}{\mu_{1}-\mu_{2}}$
(4) $\frac{2 R}{\mu_{1}-\mu_{2}}$

Sol. 3
$\frac{1}{f_{1}}=\left(\mu_{1}-1\right)\left(\frac{1}{\infty}-\frac{1}{-R}\right)=\frac{\mu_{1}-1}{R}$
$\frac{1}{f_{2}}=\left(\mu_{2}-1\right)\left(\frac{1}{-R}-\frac{1}{\infty}\right)=\frac{\mu_{2}-1}{R}$
$\frac{1}{f_{e q}}=\left(\frac{\mu_{1}-1}{R}\right)+\left(\frac{\mu_{2}-1}{-R}\right)$
$f_{e q}=\frac{R}{\left(\mu_{1}-\mu_{2}\right)}$
24. A $25 \times 10^{-3} \mathrm{~m}^{3}$ volume cylinder is filled with 1 mol of $\mathrm{O}_{2}$ gas at room temperature (300K). The molecular diameter of $\mathrm{O}_{2}$, and its root mean square speed, are found t be 0.3 nm and $200 \mathrm{~m} / \mathrm{s}$, respectively. What is the average collision rate (per second) for an $\mathrm{O}_{2}$ molecule?
(1) $\sim 10^{12}$
(2) $\sim 10^{10}$
(3) $\sim 10^{11}$
(4) $\sim 10^{13}$

## Sol. 1

collision frequency $=\sqrt{\frac{8 \mathrm{KT}}{\pi \mathrm{m}}} \frac{\sqrt{2} \pi \mathrm{~d}^{2} \mathrm{~N}_{\mathrm{A}} \mathrm{P}}{\mathrm{RT}}$
$=2.9 \times 10^{7} \mathrm{~s}^{-1}$
25. The displacement of a damped harmonic oscillator is given by
$x(t)=e^{-0.1 t} \cos (10 \pi t+\phi)$. Here $t$ is in seconds.
The time taken for its amplitude of vibration to drop to half of its initial value is close to :
(1) 27 s
(2) 7 s
(3) 13 s
(4) 4 s

Sol. 2
$x=e^{-0.1 t} \cos (10 \pi t+\phi)$
$A \longrightarrow A / 2$
$\mathrm{A}=\mathrm{A}_{0} \mathrm{e}^{-\mathrm{bt}}$ where $\mathrm{b}=0.1$
$\frac{A_{0}}{2}=A_{0} \cdot e^{-b t}$
$\mathrm{t}=\frac{\ln 2}{\mathrm{~b}}=10 \ln 2=6.93 \simeq 7 \mathrm{~s}$

## हमारा विश्वास... हर एक विद्यार्यी है ख़ास

26. A uniformly charged ring of radius 3 a and total charge $q$ is placed in $x y$-plane centred at origin. A point charge $q$ is moving towards the ring along the $z$-axis and has speed $v$ at $z=4 a$. The minimum value of $v$ such that it crosses the origin is :
(1) $\sqrt{\frac{2}{m}}\left(\frac{4}{15} \frac{q^{2}}{4 \pi \varepsilon_{0} a}\right)^{1 / 2}$
(2) $\sqrt{\frac{2}{m}}\left(\frac{2}{15} \frac{\mathrm{q}^{2}}{4 \pi \varepsilon_{0} a}\right)^{1 / 2}$
(3) $\sqrt{\frac{2}{m}}\left(\frac{1}{15} \frac{q^{2}}{4 \pi \varepsilon_{0} a}\right)^{1 / 2}$
(4) $\sqrt{\frac{2}{m}}\left(\frac{1}{5} \frac{\mathrm{q}^{2}}{4 \pi \varepsilon_{0} a}\right)^{1 / 2}$

## Soll. 2


$z=4 a$
$v=\frac{k q}{5 a}$
$U_{i}=\frac{k q^{2}}{(5 a)}$
$U_{f}=\frac{k q^{2}}{(3 a)}$
$\frac{1}{2} m v^{2}=\left(\frac{1}{3}-\frac{1}{5}\right) \frac{k q^{2}}{5 a}$
$\frac{m v^{2}}{2}=\frac{2}{15} \frac{K q^{2}}{5 a}$
$v=\sqrt{\frac{4}{15} \frac{\mathrm{kq}^{2}}{\mathrm{ma}}}$
27. A proton, an electron, and a Helium nucleus, have the same energy. They are in circular orbits in a plane due to magnetic field perpendicular to the plane Let $r_{p}, r_{e}$ and $r_{\mathrm{He}}$ be their respective radii, then,
(1) $r_{e}>r_{p}>r_{\text {He }}$
(2) $r_{e}<r_{p}<r_{\text {He }}$
(3) $r_{e}>r_{p}=r_{\text {He }}$
(4) $r_{e}<r_{p}=r_{\text {He }}$
$\mathrm{Pe}^{-} \mathrm{H}_{\mathrm{e}}^{++}$

Sol. 4
$r=\frac{m u}{q(B)}$
$r=\frac{\sqrt{2 m K}}{q B}$
$K \rightarrow$ same
$r \propto \frac{\sqrt{m}}{q}$
$B \rightarrow$ same

## हमारा विश्वास... हर एक विद्यार्यी है खुखास

$r_{1}: r_{2}: r_{3}=\frac{\sqrt{m}}{e}: \frac{\sqrt{m / 2000}}{e}: \frac{\sqrt{4 m}}{2 e}$
$\frac{\sqrt{m}}{e}: \frac{\sqrt{m} / e}{\sqrt{2000}}: \sqrt{\frac{m}{e}}$
$=1: \frac{1}{\sqrt{2000}}: 1$
i.e., $r_{p}=r_{\text {He }}>r_{e}$
28. A moving coil galvanometer allows a full scale current of $10^{-4} \mathrm{~A}$. A series resistance of $2 \mathrm{M} \Omega$ is required to convert the above galvanometer into a voltmeter of range 0-5 V. Therefore the value of shunt resistance required to convert the above galvanometer into an ammeter of range 0-10 mA is :
(1) $10 \Omega$
(2) $500 \Omega$
(3) $100 \Omega$
(4) $200 \Omega$

## Sol. Wrong

29. A stationary source emits sound waves of frequency 500 Hz . Two observers moving along a linepassing through the source detect sound to be of frequencies 480 Hz and 530 Hz . Their respective speeds area, in $\mathrm{ms}^{-1}$, (Given speed of sound $=300 \mathrm{~m} / \mathrm{s}$ )
(1) 16,14
(2) 12,16
(3) 8,18
(4) 12,18

Sol. 4
$f=500 \mathrm{~Hz}(u=0)$
$f_{5 / 1}=480 H z f_{5 / 2}=530$
$f_{5 / 1}=\left(\frac{300-V_{1}}{300}\right) 500=480 \&\left(\frac{300+V_{B}}{300}\right) 500=530$
$V_{1}=12 \mathrm{~m} / \mathrm{s}$ and $\mathrm{V}_{2}=18 \mathrm{~m} / \mathrm{s}$
30. Two wires $A \& B$ are carrying currents $I_{1} \& I_{2}$ as shown in the figure. The separation between them is d. A third wire C carrying a current $I$ is to be kept parallel to them at a distance $x$ from $A$ such that the net force acting on it is zero. The possible values of $x$ are :

(1) $x=\left(\frac{I_{2}}{I_{1}+I_{2}}\right) d$ and $x=\left(\frac{I_{2}}{I_{1}-I_{2}}\right) d$
(2) $x=\left(\frac{I_{1}}{I_{1}+I_{2}}\right) d$ and $x=\frac{I_{2}}{\left(I_{1}-I_{2}\right)} d$
(3) $x= \pm \frac{I_{1} d}{\left(I_{1}-I_{2}\right)}$
(4) $x=\left(\frac{I_{1}}{I_{1}-I_{2}}\right) d$ and $x=\frac{I_{2}}{\left(I_{1}+I_{2}\right)} d$

Sol. 3

## मोशन ने बनाया साधारण को असाधारण JEE Main Result Jan'19 <br> 4 RESIDENTIAL COACHING PROGRAM (DRONA) STUDENTS ABOVE 99.9 PERCENTILE



Total Students Above 99.9 percentile - 17
Total Students Above 99 percentile - 282
Total Students Above 95 percentile - 983
\% of Students Above 95 percentile $\frac{983}{3538}=$ $=$ 2 27 .78\%

Scholarship on the Basis of 12th Class Result

| Marks <br> PCM or PCB | Hindi State <br> Board | State Eng <br> OR CBSE |
| :--- | :---: | :---: |
| $\mathbf{7 0 \% - 7 4 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{2 0 \%}$ |
| $\mathbf{7 5 \% - 7 9 \%}$ | $\mathbf{3 5 \%}$ | $\mathbf{2 5 \%}$ |
| $\mathbf{8 0 \% - 8 4 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{3 5 \%}$ |
| $85 \%-87 \%$ | $\mathbf{5 0 \%}$ | $\mathbf{4 0 \%}$ |
| $88 \%-90 \%$ | $\mathbf{6 0 \%}$ | $\mathbf{5 5 \%}$ |
| $\mathbf{9 1 \% - 9 2 \%}$ | $\mathbf{7 0 \%}$ | $\mathbf{6 5 \%}$ |
| $\mathbf{9 3 \% - 9 4 \%}$ | $\mathbf{8 0 \%}$ | $\mathbf{7 5 \%}$ |
| $\mathbf{9 5 \%}$ \& Above | $\mathbf{9 0 \%}$ | $\mathbf{8 5 \%}$ |

New Batches for Class $11^{\text {th }}$ to $12^{\text {th }}$ pass
17 April 2019 \& 01 May 2019
हिन्दी माध्यम 市 लिए पृथात बैच

| Scholarship on the Basis of JEE Main Percentile |  | English Medium | Hindi Medium |
| :---: | :---: | :---: | :---: |
| Score | JEE Mains Percentile | Scholarship | Scholarship |
| 225 Above | Above 99 | Drona Free | mited Seats) |
| 190 to 224 | Above 97.5 To 99 | 100\% | 100\% |
| 180 to 190 | Aboev 97 To 97.5 | 90\% | 90\% |
| 170 to 179 | Above 96.5 To 97 | 80\% | 80\% |
| 160 to 169 | Above 96 To 96.5 | 60\% | 60\% |
| 140 to 159 | Above 95.5 To 96 | 55\% | 55\% |
| 74 to 139 | Above 95 To 95.5 | 50\% | 50\% |
| 66 to 73 | Above 93 To 95 | 40\% | 40\% |
| 50 to 65 | Above 90 To 93 | 30\% | 35\% |
| 35 to 49 | Above 85 To 90 | 25\% | 30\% |
| 20 to 34 | Above 80 To 85 | 20\% | 25\% |
| 15 to 19 | 75 To 80 | 10\% | 15\% |

