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## हमारा विश्वास... हर एक विद्यार्यी है खुास

## Motion

1. A Thin strip 10 cm long is on a $U$ shaped wire of negligible resistance and it is connected to a spring of spring constant $0.5 \mathrm{Nm}^{-1}$ (see figure). The assembly is kept in a uniform magnetic field of 0.1 T . If the stripe is pulled from its equilibrium position and released, the number of oscillations it performs before its amplitude decreases by a factor of e is $N$. If the mass of the strip is 50 grams, its resistance $10 \Omega$ and air drag negligible, N will be close to :

(1) 10000
(3) 1000
(2) 5000
(4) 50000

Sol. 2
$A=A_{0} e^{-\frac{b}{2 m} t}$
$\varepsilon=u B I$
$\mathrm{F}=\mathrm{Bil}$
$i=\frac{\varepsilon}{R}=\frac{u B I}{R}$
$F=\frac{B^{2} v l^{2}}{R}$
$m a=\frac{B^{2} l^{2}}{R} v+k x$
$a=\frac{\left.B^{2}\right|^{2}}{m R} v+\frac{k x}{m}$
$\frac{d^{2} x}{d t^{2}}-\frac{B^{2} l^{2}}{m R} \frac{d x}{d t}-k x=0$
$\left(\frac{b}{2 m}\right) t=1 \quad A=\left(\frac{A_{0}}{e}\right)$
$t \frac{B^{2} I^{2}}{2 m R}=1 \quad t=\frac{2 m R}{\left.B^{2}\right|^{2}}$
$\mathrm{t}=\frac{2 \times 50 \times 10^{-3} \times 10}{0.1 \times 0.1 \times 0.1 \times 0.1}$
$\mathrm{t}=10,000 \mathrm{sec}$
$T=2 \pi \sqrt{\frac{\mathrm{~m}}{\mathrm{k}}}$
$\mathrm{T}=2 \pi \sqrt{\frac{50 \times 10^{-3}}{0.5}}$
$T=\frac{2 \pi}{\sqrt{10}}$
$N=\frac{t}{T}$
$N=\frac{10000}{2}=5000$

## हमारा विश्वास... हर एक विद्यार्थी है ख़ास

2. A thermally insulated vessel contains 150 g of water at $0^{\circ} \mathrm{C}$. then the air from the vessel is pumped out adiabatically. A fraction of water turns into ice and the rest evaporates at $0^{\circ} \mathrm{C}$ itself. The mass of evaporated water will be closest to :
(Latent heat of vaporization of water $=2.10 \times 10^{6} \mathrm{~J} \mathrm{~kg}^{-1}$ and Latent heat of Fusion of water $=$ $3.36 \times 10^{5} \mathrm{~J} \mathrm{~kg}^{-1}$ )
(1) 150 g
(2) 35 g
(3) 20 g
(4) 130 g

Sol. 3

| Vapour |
| :---: |
| $x$ |
| ice |
| $(150-x)$ |

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\(x L_{v}=(150-x) L_{f}\)
\(x 2.10 \times 10^{6}=(150-x) 3.36 \times 10^{5}\)
\(x=20 \mathrm{gm}\)
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3. In SI units, the dimensions of $\sqrt{\frac{\epsilon_{0}}{\mu_{0}}}$ is :
(1) $A T^{2} M^{-1} L^{-1}$
(2) $A T^{-3} M L^{3 / 2}$
(3) $\mathrm{A}^{-1} \mathrm{TML}^{3}$
(4) $A^{2} T^{3} M^{-1} L^{-2}$

Sol. 4
$C=\frac{1}{\sqrt{\mu_{0} \varepsilon_{0}}}$
$\sqrt{\frac{\varepsilon_{0}}{\mu_{0}}}=\varepsilon_{0} \frac{1}{\sqrt{\mu_{0} \varepsilon_{0}}}=\varepsilon_{0} C$
$F=\frac{1}{4 \pi \varepsilon_{0}} \frac{q^{2}}{r^{2}}$
$\varepsilon_{0}=\frac{\mathrm{q}^{2}}{4 \pi \mathrm{Fr}^{2}}=\frac{\mathrm{I}^{2} \mathrm{t}^{2}}{4 \pi \mathrm{Fr}^{2}}$
$=\frac{\mathrm{I}^{2} \mathrm{t}^{2}}{4 \pi \mathrm{Fr}^{2}} \mathrm{C}$
$=\frac{A^{2} T^{2} L T^{-1}}{M L T^{-2} L^{2}}=M^{-1} L^{-2} T^{-3} A^{2}$
4. A thin circular plate of mass $M$ and radius $R$ has its density varying as $p(r)=\rho_{0} r$ with $\rho_{0}$ as constant and $r$ is the distance from its center. The moment of inertia of the circular plate about an axis perpendicular to the plate and passing through its edge is $I=a M R^{2}$. The value of the coefficient a is :
(1) $\frac{8}{5}$
(2) $\frac{3}{2}$
(3) $\frac{1}{2}$
(4) $\frac{3}{5}$

## हमारा विश्वास... हू प्त विद्यार्यी है खुास

Sol. 1

$\mathrm{dm}=\rho 2 \pi \mathrm{rdr}$
$\mathrm{dm}=\rho_{0} \mathrm{r} 2 \pi \mathrm{rdr}$
$d m=2 \pi \rho_{0} r^{2} d r$
$\mathrm{dI}=\mathrm{dmr}^{2}$
$\int d I=2 \pi \rho_{0} \int_{0}^{R} r^{4} d r$
$\mathrm{I}=2 \pi \rho_{0} \frac{\mathrm{R}^{5}}{5}$
$\int d m=\rho_{0} 2 \pi \int_{0}^{R} r^{2} d r$
$M=2 \pi \rho_{0} \frac{R^{3}}{3}$
$2 \pi \rho_{0}=\left(\frac{3 M}{R^{3}}\right)$
$I=\frac{3 M}{R^{3}} \frac{R^{5}}{5}=\frac{3}{5} M R^{2}$
$I=M R^{2}+\frac{3}{5} M R^{2}=\frac{8}{5} M R^{2}$
5. An alternating voltage $v(t)=220 \sin 100 \pi t$ volt is applied to a purely resistive load of $50 \Omega$. The time taken for the current to rise from half of the peak value to the peak value is :
(1) 5 ms
(2) 2.2 ms
(3) 7.2 ms
(4) 3.5 ms

Sol. 4
$u=220 \sin (100 \pi t)$

$\mathrm{w}=100 \pi$
$\mathrm{t}=\mathrm{T} / 6$
$\frac{2 \pi}{\mathrm{~T}}=100 \pi$
$T=\frac{2}{100}=\frac{1}{50}$

## हमारा विश्वास... हा एक विद्यार्यी है खुास

$t=\frac{1}{300} \mathrm{sec}$
$\mathrm{t}=0.33 \times 10^{-2} \mathrm{sec}$
$=3.3 \times 10^{-3} \mathrm{sec}$
6. For the circuit shown, with $R_{1}=1.0 \Omega, R_{2}=2.0 \Omega, E_{1}=2 \mathrm{~V}$ and $E_{2}=E_{3}=4 \mathrm{~V}$, the potential difference between the points ' $a$ ' and ' $b$ ' is approximately (in V ) :

(1) 2.7
(2) 3.3
(3) 2.3
(4) 3.7

Sol. 2

$\frac{x-2}{2}+\frac{x-4}{2}+\frac{x-4}{2}=0$
$3 x=10$
$x=\frac{10}{3}$
$\mathrm{V}=\frac{10}{3}=3.3$ volt
7. In figure, the optical fiber is $I=2 \mathrm{~m}$ long and has a diameter of $\mathrm{d}=20 \mu \mathrm{~m}$. If a ray of light is incident on one end of fiber at angle $\theta_{1}=40^{\circ}$, the number of reflections it makes before emerging from the other end is close to :
(refractive index of fiber is 1.31 and $\sin 40^{\circ}=0.64$ )

(1) 55000
(2) 45000
(3) 66000
(4) 57000

## हमारा विश्वास... हा पक विस्यार्थी है खुखास

Sol. 4

$1 \sin 40=\mu \sin \theta_{2}$
$0.64=1.31 \sin \theta_{2}$
$\sin \theta_{2}=\frac{0.64}{1.31}=0.5 \theta_{2}=30^{\circ}$
$\tan 30^{\circ}=\frac{d}{x} \quad x=\frac{d}{\tan 30^{\circ}}$
$x=20 \times 10^{-6} \sqrt{3}$
$\mathrm{n}=\frac{\mathrm{l}}{\mathrm{x}}$
$\mathrm{n}=\frac{2}{20 \times 10^{-6} \times 1.732}$
$\mathrm{n}=\frac{1}{1.732} \times 10^{5}=57736$
8. The reverse breakdown voltage of a Zener diode is 5.6 V in the given circuit.


The current $\mathrm{I}_{\mathrm{z}}$ through the Zener is :
(1) 10 mA
(2) 7 mA
(3) 17 mA
(4) 15 mA

Sol. 1
$\mathrm{i}_{800 \Omega}=\frac{5.6}{800} \mathrm{amp}=0.007 \mathrm{amp}$
$\mathrm{i}_{200 \Omega}=\frac{3.4}{200} \mathrm{amp}=0.017 \mathrm{amp}$
$i_{\text {diode }}=i_{200 \Omega}-i_{800 \Omega}$
$=0.017-0.007$
$=0.01 \mathrm{amp}$
$=10 \mathrm{~mA}$
9. A boy's catapult is made of rubber cord which is 42 cm long, with 6 mm diameter of cross-section and of negligible mass. The boy keeps a stone weighing 0.02 kg on it and stretches the cord by 20 cm by applying a constant force. When released, the stone flies off with a velocity of $20 \mathrm{~ms}^{-}$ ${ }^{1}$. Neglect the change in the area of cross-section of the cord while stretched. The Young's modulus of rubber is closest to :
(1) $10^{6} \mathrm{Nm}^{-2}$
(2) $10^{3} \mathrm{Nm}^{-2}$
(3) $10^{4} \mathrm{Nm}^{-2}$
(4) $10^{8} \mathrm{Nm}^{-2}$

## हमारा विश्वास... ही एक विद्यार्यी है खुल

## Sol. 1

$\frac{\mathrm{U}}{\mathrm{V}}=\frac{1}{2}$ stress $\times$ strain
$Y=\frac{\text { Stress }}{\text { Strain }}$
Stress $=\mathrm{Y}$ strain
$\frac{\mathrm{U}}{\mathrm{V}}=\frac{1}{2} \mathrm{Y} \times(\text { Strain })^{2}$
$\frac{1}{2} m v^{2}=\frac{1}{2} Y\left(\frac{\Delta I}{I}\right)^{2} A . L$
$Y=\frac{m v^{2} I^{2}}{(\Delta I)^{2} A . L}=\frac{0.002 \times 400 \times 42 \times 42 \times 10^{-4}}{20 \times 20 \times 10^{-4} \times \pi 9 \times 10^{-6} 42 \times 10^{-2}}$
$Y=\frac{42 \times 10^{6} \times 2}{9 \times 3.14}=2.97 \times 10^{6} \mathrm{~N} / \mathrm{m}^{2}$
10. A solid conducting sphere, having a charge $Q$, is surrounded by an uncharged conducting hollow spherical shell. Let the potential difference between the surface of the solid sphere and that of the outer surface of the hollow shell be $V$. If the shell is now given a charge of -4 Q , the new potential difference between the same two surfaces is :
(1) 4 V
(2) 2 V
(3) V
(4) -2 V

## Sol. 3


$\Delta \mathrm{V}=\mathrm{V}_{1}-\mathrm{V}_{2}=\mathrm{V}$

$\Delta V=V_{1}-V-V_{2}+V$
$\Delta V=V_{1}-V_{2}=V$
No change

## हमारा विश्वास... हर एक विद्यार्यी है ख़ास

11. Four identical particles of mass $M$ are located at the corners of a square of side 'a'. What should be their speed if each of them revolves under the influence of other's gravitational field in a circular orbit circumscribing the square ?

(1) $1.35 \sqrt{\frac{G M}{a}}$
(2) $1.21 \sqrt{\frac{G M}{a}}$
(3) $1.41 \sqrt{\frac{G M}{a}}$
(4) $1.16 \sqrt{\frac{\mathrm{GM}}{\mathrm{a}}}$

Sol. 4

$\frac{M v^{2}}{\left(\frac{a}{\sqrt{2}}\right)}=\frac{G m^{2}}{2 a^{2}}+\frac{\sqrt{2} G m^{2}}{a^{2}}$
$v^{2}=\frac{G m}{a^{2}}(0.5+1.41) \frac{a}{\sqrt{2}}$
$\mathrm{v}^{2}=\frac{\mathrm{Gm}}{\mathrm{a}}\left(\frac{1.91}{1.41}\right)$
$v=\sqrt{\frac{1.91}{1.41}} \sqrt{\frac{\mathrm{Gm}}{\mathrm{a}}}=\sqrt{1.35} \sqrt{\frac{\mathrm{Gm}}{\mathrm{a}}}$
$v=1.16 \sqrt{\frac{G m}{a}}$
12. The wavelength of the carrier waves in a modern optical fiber communication network is close to :
(1) 900 nm
(2) 2400 nm
(3) 600 nm
(4) 1500 nm

## Sol. 4

Wave length of carrier wave in optical cable fibre is 1500 nm
13. Voltage rating of a parallel plate capacitor is 500 V . its dielectric can withstand a maximum electric field of $10^{6} \mathrm{~V} / \mathrm{m}$. The plate area is $10^{-1} \mathrm{~m}^{2}$. What is the dielectric constant if the capacitance is 15 pF ?
(given $\epsilon_{0}=8.86 \times 10^{-12} \mathrm{C}^{2} / \mathrm{Nm}^{2}$ )
(1) 8.5
(2) 6.2
(3) 4.5
(4) 3.8

## हमारा विश्वास... हा एक विद्यार्यी है खुास

Sol. 1
$V=E d$
$d=\frac{V}{E}$
$C=k \varepsilon_{0} \frac{A}{d}$
$k=\frac{C d}{\varepsilon_{0} A}$
$k=\frac{C V}{\varepsilon_{0} A E}$
$\mathrm{k}=\frac{15 \times 10^{-12} \times 500}{8.86 \times 10^{-12} \times 10^{-4} \times 10^{6}}$
$k=\frac{75}{8.86}=8.46 \approx 8.5$
14. A particle moves in one dimension from rest under the influence of a force that varies with the distaance travelled by the particle as shown in the figure. The kinetic energy of the particle after it has travelled 3 m is :

(1) 4 J
(2) 5 J
(3) 6.5 J
(4) 2.5 J

## Sol. 3

$2 \times 2+\frac{1}{2}(2+3)(3-2)=K E$
$4+\frac{5}{2}=K E$
$4+2.5=K E$
$\mathrm{K}=6.5 \mathrm{~J}$
15. A 20 Henry inductor coil is connected to a 10 ohm resitsance in series as shown in figure. The time at which rate of dissipation of energy (joule's heat) across resistance is equal to the rate at which magnetic energy is store in the inductor, is :

(1) $\frac{2}{\ln 2}$
(2) $\ln 2$
(3) $2 \ln 2$
(4) $\frac{1}{2} \ln 2$

## हमारा विश्वास... हा एक निद्यार्थी है ख़्वास

## Sol. 3

$i=i_{0}\left(1-e^{\frac{R_{t}}{\mathrm{~L}}}\right)$
$\mathrm{E}=\frac{1}{2} \mathrm{Li}{ }^{2}$
$\frac{\mathrm{dE}}{\mathrm{dt}}=\frac{1}{2} \mathrm{~L} 2 \mathrm{i} \frac{\mathrm{di}}{\mathrm{dt}}=\mathrm{Li} \frac{\mathrm{di}}{\mathrm{dt}}$
$\frac{d i}{d t}=i_{0} \frac{R}{L} \quad e^{-\frac{R}{L} t}$
$\frac{\mathrm{dE}}{\mathrm{dt}} \Rightarrow \mathrm{Li} \quad \mathrm{i}_{0} \frac{R}{\mathrm{~L}} \mathrm{e}^{-\frac{R}{\mathrm{~L}} \mathrm{t}}=\mathrm{i}^{2} R$
$\Rightarrow \mathrm{i}_{0} e^{-\frac{R}{L} t}=\mathrm{i}_{0}-\mathrm{i}_{0} e^{-\frac{R_{t}}{L} t}$
$2 e^{-\frac{R}{L} t}=1$
$\frac{R}{L} t=\operatorname{Ln} 2$
$t=\frac{L}{R} \ln (2)=2 \operatorname{Ln}(2)$
16. Two identical beakers $A$ and $B$ contain equal volumes of two different liquids at $60^{\circ} \mathrm{C}$ each and left to cool down. Liquid in A has density of $8 \times 10^{2} \mathrm{~kg} / \mathrm{m}^{3}$ and specific heat of $2000 \mathrm{~J} \mathrm{~kg}^{-1} \mathrm{~K}^{-1}$ while liquid in $B$ has density of $10^{3} \mathrm{kgm}^{-3}$ and specific heat of $4000 \mathrm{~J} \mathrm{~kg}^{-1} \mathrm{~K}^{-1}$. Which of the following best describes their temperature versus time graph schematically ? (assume the emissivity of both the beakers to be the same)
(1)

(2)

(3)

(4)


Sol. 4
(-) $\frac{d T}{d t}=\frac{\sigma A .4 T_{0}^{3}}{m \rho}\left(T-T_{0}\right)$
$(-) \frac{\mathrm{dT}}{\mathrm{dt}}=\frac{4 \sigma \mathrm{~T}_{0}^{3} \cdot \mathrm{~A}}{\mathrm{vd} \rho}\left(\mathrm{T}-\mathrm{T}_{0}\right)$
(-) $\frac{\mathrm{dT}}{\mathrm{dt}}=\frac{1}{\mathrm{~d} \rho} \mathrm{~K} \quad \mathrm{~K}=\frac{4 \sigma \mathrm{~T}_{0}^{3} \mathrm{~A}\left(\mathrm{~T}-\mathrm{T}_{0}\right)}{\mathrm{V}}$
$\left(-\frac{\mathrm{dT}}{\mathrm{dt}}\right)_{A}=\frac{1}{16 \times 10^{5}} \mathrm{~K}=-0.0625 \times 10^{-5} \mathrm{~K}$

## हमारा विश्वास... ह एक विद्यार्यी है खुास

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\(\left(-\frac{\mathrm{dT}}{\mathrm{dt}}\right)_{B}=\frac{1}{40 \times 105} \mathrm{~K}=-0.02510^{-54} \mathrm{~K}\)
\(\tan \theta_{\mathrm{A}}>\tan \theta_{\mathrm{B}}\)
\(\theta_{\mathrm{B}}>\theta_{\mathrm{A}}\)
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17. An upright object is placed at a distance of 40 cm in front of a convergent lens of focal length 20 cm . A convergent mirror of focal length 10 cm is placed at a distance of 60 cm on the other side of the lens. the position and size of the final image will be :
(1) 20 cm from the convergent mirror, twice the size of the object
(2) 20 cm from the convergent mirror, same size as the object
(3) 40 cm from the convergent mirror, same size as the object
(4) 40 cm from the convergent lens, twice the size of the object

## Sol. (Bonus)



Ist refraction $u=-40 \mathrm{~cm} ; \mathrm{f}=+20 \mathrm{~cm}$
$\Rightarrow \mathrm{v}=+40 \mathrm{~cm}$ (image $\mathrm{I}_{1}$ )
and $m_{1}=-1$
for reflection
$\mathrm{u}=-20 \mathrm{~cm} ; \mathrm{f}=-10 \mathrm{~cm}$
$\Rightarrow \mathrm{v}=-20 \mathrm{~cm}$ (image $\mathrm{I}_{2}$ )
and $m_{2}=-1$
$2^{\text {nd }}$ refraction
$u=-40 \mathrm{~cm} ; \mathrm{f}=+20 \mathrm{~cm}$
$\Rightarrow \mathrm{v}=+40 \mathrm{~cm}$ (image $\mathrm{I}_{3}$ )
and $m_{3}=-1$
Total magnification $=m_{1} \times m_{2} \times m_{3}=-1$
and final image is formed at distance 40 cm from convergent lens and is of same size as the object.
18. A plane electromagnetic wave travels in free space along the x-direction. the electric field component of the wave at a particular point of space and time is $E=6 \mathrm{Vm}^{-1}$ along $y$-direction. its corresponding magnetic field component, B would be :
(1) $6 \times 10^{-8} \mathrm{~T}$ along z-direction
(2) $2 \times 10^{-8} \mathrm{~T}$ along z-direction

## हमारा विश्वास... हा एक विद्यार्यी है खुास

(3) $2 \times 10^{-8} \mathrm{~T}$ along $y$-direction
(4) $6 \times 10^{-8} \mathrm{~T}$ along x -direction

Sol. 2
$E=B C$
$B=\frac{E}{C}=\frac{6}{3 \times 10^{8}}$
$B=2 \times 10^{-8}$

19. Four particles $A, B, C$ and $D$ with masses $m_{A}=m, m_{B}=2 m, m_{C}=3 m$ and $m_{D}=4 m$ are at the corners of a square. They have accelerations of equal magnitude with directions as shown. The acceleration of the centre of mass of the particles is :

(1) $\frac{a}{5}(\hat{i}-\hat{j})$
(2) Zero
(3) $a(\hat{i}+\hat{j})$
(4) $\frac{a}{5}(\hat{i}+\hat{j})$

Sol. 1
$a_{c m}=\frac{-m a \hat{i}+3 m a \hat{i}+2 m a \hat{j}-4 m a \hat{j}}{10 m}$
$a_{c m}=\frac{2 m a \hat{i}-2 m a \hat{j}}{10 m}=\frac{a}{5}(\hat{i}-\hat{j})$
20. A wire of length $2 L$, is made by joining two wires $A$ and $B$ of same length but different radii $r$ and $2 r$ and made of the same material. It is vibrating at a frequency such that the joint of the two wires forms a node. If the number of antinodes in wire $A$ is $p$ and that in $B$ is $q$ then the ratio $p: q$ is :

(1) $1: 2$
(2) $1: 4$
(3) $3: 5$
(4) $4: 9$

## हमारा विश्वास... हर एक विद्यार्यी है खुास

Sol. 1

$f=\frac{p}{2 l} \sqrt{\frac{T}{\mu_{1}}}=\frac{q}{2(I)} \sqrt{\frac{T}{\mu_{2}}}$
$\frac{p}{q}=\sqrt{\frac{\mu_{1}}{\mu_{2}}}=\sqrt{\frac{A_{1}}{A_{2}}}=\sqrt{\frac{\pi r^{2}}{\pi 4 r^{2}}}$
$\frac{p}{q}=\frac{1}{2}$
21. A circular coil having $N$ turns and radius $r$ carries a current $I$. It is held in the $X Z$ plane in a magnetic field $\mathrm{B} \hat{\mathrm{i}}$. The torque on the coil due to the magnetic field is :
(1) $\mathrm{B} \pi \mathrm{r}^{2} \mathrm{I} \mathrm{N}$
(2) $\frac{B \pi r^{2} I}{N}$
(3) Zero
(4) $\frac{\mathrm{Br}^{2} \mathrm{I}}{\pi \mathrm{N}}$

Sol. 1

$Z=M B \sin 90$
$Z=\operatorname{NiA} \frac{\mu_{0} \mathrm{Ni}}{2 r}$
$Z=N i \pi r^{2} B$
22. Two particles move at right angle to each other. Their de Broglie wavelengths are $\lambda_{1}$ and $\lambda_{2}$ respectively. The particles suffer perfectly inelastic collision. The de Broglie wavelength $\lambda$, of the final particle, is given by :
(1) $\lambda=\sqrt{\lambda_{1} \lambda_{2}}$
(2) $\frac{1}{\lambda^{2}}=\frac{1}{\lambda_{1}^{2}}+\frac{1}{\lambda_{2}^{2}}$
(3) $\lambda=\frac{\lambda_{1}+\lambda_{2}}{2}$
(4) $\frac{2}{\lambda}=\frac{1}{\lambda_{1}}+\frac{1}{\lambda_{2}}$

## Sol. 2


$\vec{P}=P_{1} \hat{i}+P_{2} \hat{j}$
$P^{2}=P_{1}{ }^{2}+P_{2}{ }^{2}$

## हमारा विश्वास... हर एक विद्यार्यी है ख़ास

$P=\sqrt{P_{1}^{2}+P_{2}^{2}}$
$\frac{1}{\lambda^{2}}=\frac{1}{\lambda_{1}^{2}}+\frac{1}{\lambda_{2}^{2}}$
23. In an interference experiment the ratio of amplitudes of coherent waves is $\frac{a_{1}}{a_{2}}=\frac{1}{3}$. The ratio of maximum and minimum intensities of fringes will be :
(1) 4
(2) 9
(3) 2
(4) 18

Sol. 1
$a_{2}=3 a_{1}$
$\frac{I_{\text {max }}}{I_{\text {min }}}=\left(\frac{\sqrt{I_{1}}+\sqrt{I_{2}}}{\sqrt{I_{1}}-\sqrt{I_{2}}}\right)^{2}$
$I \propto a^{2}$
$\frac{I_{1}}{I_{2}}=\left(\frac{a_{1}}{a_{2}}\right)^{2}=\frac{1}{9}$
$I_{2}=9 I_{1}$
$\frac{I_{\text {max }}}{I_{\text {min }}}=\left(\frac{4}{2}\right)^{2}=\left(\frac{4}{1}\right)$
24. A $200 \Omega$ resistor has a certain color code. If one replaces the red color by green in the code, the new resistance will be :
(1) $300 \Omega$
(2) $100 \Omega$
(3) $400 \Omega$
(4) $500 \Omega$

Sol. 1
Red Black Brown

| R | $=10$ |
| :--- | :--- | :--- |
| $20 \times 10=200 \Omega$ |  |

Green Black Brown

25. Ship $A$ is sailing towards north-east with velocity $\vec{v}=30 \hat{i}+50 \hat{j} \mathrm{~km} / \mathrm{hr}$ where $\hat{i}$ points east and $\hat{j}$, north. Ship B is at a distance of 80 km east and 150 km north of ship A and is sailing towards west at $10 \mathrm{~km} / \mathrm{hr}$. A will be at minimum distance from $B$ in :
(1) 4.2 hrs .
(2) 2.2 hrs .
(3) 2.6 hrs
(4) 3.2 hrs .

Sol. 3
$\vec{V}_{r}=40 \hat{i}-50 \hat{j}$
$\vec{r}_{e}=-80 \hat{i}-150 \hat{j}$

## हमारा विश्वास... हा एक विद्यार्यी है खुास

$t=\frac{\left|\vec{V}_{r} \cdot \vec{r}\right|}{\left|\vec{V}_{r}\right|^{2}}=\frac{10700}{4100}=\frac{107}{41}=2.6 \mathrm{sec}$
26. The bob of a simple pendulum has mass 2 g and a charge of $5.0 \mu \mathrm{C}$. It is at rest in a uniform horizontal electric field of intensity $2000 \mathrm{~V} / \mathrm{m}$. At equilibrium, the angle that the pendulum makes with the vertical is :
(take $\mathrm{g}=10 \mathrm{~m} / \mathrm{s}^{2}$ )
(1) $\tan ^{-1}(5 .-0)$
(2) $\tan ^{-1}(2.0)$
(3) $\tan ^{-1}(0.2)$
(4) $\tan ^{-1}(0.5)$

Sol. 4
$\mathrm{T} \sin \theta=\mathrm{qE}$
$\mathrm{T} \cos \theta=\mathrm{mg}$
$\tan \theta=\frac{\mathrm{qE}}{\mathrm{mg}}$
$\tan \theta=\frac{5 \times 10^{-6} \times 2000}{2 \times 10^{-3} \times 10}$
$\theta=\tan ^{-1}(0.5)$

27. A steel wire having a radius of 2.0 mm , carrying a load of 4 kg , is hanging from a ceiling. Given that $\mathrm{g}=3.1 \pi \mathrm{~ms}^{-2}$, what will be the tensile stress that would be developed in the wire ?
(1) $3.1 \times 10^{6} \mathrm{Nm}^{-2}$
(2) $5.2 \times 10^{6} \mathrm{Nm}^{-2}$
(3) $6.2 \times 10^{6} \mathrm{Nm}^{-2}$
(4) $4.8 \times 10^{6} \mathrm{Nm}^{-2}$

Sol. 1
stress $=\frac{F}{A}$
$=\frac{4 \times 3.1 \pi}{\pi 4 \times 10^{-6}}=3.1 \times 10^{6}$
28. If $10^{22}$ gas molecules each of mass $10^{-26} \mathrm{~kg}$ collide with a surface (perpendicular to it) elastically per second over an area $1 \mathrm{~m}^{2}$ with a speed $10^{4} \mathrm{~m} / \mathrm{s}$, the pressure exerted by the gas molecules will be of the order of :
(1) $10^{3} \mathrm{~N} / \mathrm{m}^{2}$
(2) $10^{4} \mathrm{~N} / \mathrm{m}^{2}$
(3) $10^{16} \mathrm{~N} / \mathrm{m}^{2}$
(4) $10^{8} \mathrm{~N} / \mathrm{m}^{2}$

## Sol. Bonus

$F=\frac{\Delta P}{\Delta t}=2 m n v$
$P=\frac{F}{A}=\frac{2 \mathrm{mnv}}{\mathrm{A}}=\frac{2 \times 10^{-26} \times 10^{22} \times 10^{4}}{1}$
$\mathrm{P}=2 \mathrm{~N} / \mathrm{m}^{2}$
29. Radiation coming from transitions $n=2$ to $n=1$ of hydrogen atoms fall on $\mathrm{He}^{+}$ions in $n=1$ and $\mathrm{n}=2$ states. The possible transition of helium ions as they absorb energy from the radiation is:
(1) $\mathrm{n}=2 \rightarrow \mathrm{n}=5$
(2) $n=2 \rightarrow n=3$
(3) $n=1 \rightarrow n=4$ (4) $n=2 \rightarrow n=4$

Sol. 4
For hydrogen
$(\mathrm{n}=2)-3.4 \mathrm{eV}$
( $\mathrm{n}=1$ ) -13.6 eV
$\Delta \mathrm{E}=-3.4+13.6=10.2 \mathrm{eV}$
$(\mathrm{n}=4)-0.85 \times 4=-3.4 \mathrm{eV}$

## हमारा विश्वास... हा एक विद्यार्यी है खुास

$(n=3)-1.5 \times 4=-6.04 \mathrm{eV}$
$(n=2)-3.4 \times 4=-13.6 \mathrm{eV}$
$(n=1)-13.4 \times 4$
30. Water from a pipe is coming at a rate of 100 liters per minute. If the radius of the pipe is 5 cm , the Reynolds number for the flow is of the order of : (density of water $=1000 \mathrm{~kg} / \mathrm{m}^{3}$, coefficient of viscosity of water $=1 \mathrm{mPa} \mathrm{s}$ )
(1) $10^{3}$
(2) $10^{2}$
(3) $10^{4}$
(4) $10^{6}$

## Sol. 3

$\frac{d v}{d t}=A v=\frac{100 \times 10^{-3}}{60}$
$v=\frac{1}{600 \times \pi \times 25 \times 10^{-4}}$
$R=\frac{\rho V D}{\eta}=\frac{1000 \times 1 \times 10 \times 10^{-2}}{600 \times \pi \times 25 \times 10^{-4} \times 10^{-3}}$
$=2 \times 10^{4}$

## मोशन ने बनाया साधारण को असाधारण JEE Main Result Jan'19 <br> 4 RESIDENTIAL COACHING PROGRAM (DRONA) STUDENTS ABOVE 99.9 PERCENTILE



Total Students Above 99.9 percentile - 17
Total Students Above 99 percentile - 282
Total Students Above 95 percentile - 983
\% of Students Above 95 percentile $\frac{983}{3538}=$ $=$ 2 27 .78\%

Scholarship on the Basis of 12th Class Result

| Marks <br> PCM or PCB | Hindi State <br> Board | State Eng <br> OR CBSE |
| :--- | :---: | :---: |
| $\mathbf{7 0 \% - 7 4 \%}$ | $\mathbf{3 0 \%}$ | $\mathbf{2 0 \%}$ |
| $\mathbf{7 5 \% - 7 9 \%}$ | $\mathbf{3 5 \%}$ | $\mathbf{2 5 \%}$ |
| $\mathbf{8 0 \% - 8 4 \%}$ | $\mathbf{4 0 \%}$ | $\mathbf{3 5 \%}$ |
| $85 \%-87 \%$ | $\mathbf{5 0 \%}$ | $\mathbf{4 0 \%}$ |
| $88 \%-90 \%$ | $\mathbf{6 0 \%}$ | $\mathbf{5 5 \%}$ |
| $\mathbf{9 1 \% - 9 2 \%}$ | $\mathbf{7 0 \%}$ | $\mathbf{6 5 \%}$ |
| $\mathbf{9 3 \% - 9 4 \%}$ | $\mathbf{8 0 \%}$ | $\mathbf{7 5 \%}$ |
| $\mathbf{9 5 \%}$ \& Above | $\mathbf{9 0 \%}$ | $\mathbf{8 5 \%}$ |

New Batches for Class $11^{\text {th }}$ to $12^{\text {th }}$ pass
17 April 2019 \& 01 May 2019
हिन्दी माध्यम 市 लिए पृथात बैच

| Scholarship on the Basis of JEE Main Percentile |  | English Medium | Hindi Medium |
| :---: | :---: | :---: | :---: |
| Score | JEE Mains Percentile | Scholarship | Scholarship |
| 225 Above | Above 99 | Drona Free | mited Seats) |
| 190 to 224 | Above 97.5 To 99 | 100\% | 100\% |
| 180 to 190 | Aboev 97 To 97.5 | 90\% | 90\% |
| 170 to 179 | Above 96.5 To 97 | 80\% | 80\% |
| 160 to 169 | Above 96 To 96.5 | 60\% | 60\% |
| 140 to 159 | Above 95.5 To 96 | 55\% | 55\% |
| 74 to 139 | Above 95 To 95.5 | 50\% | 50\% |
| 66 to 73 | Above 93 To 95 | 40\% | 40\% |
| 50 to 65 | Above 90 To 93 | 30\% | 35\% |
| 35 to 49 | Above 85 To 90 | 25\% | 30\% |
| 20 to 34 | Above 80 To 85 | 20\% | 25\% |
| 15 to 19 | 75 To 80 | 10\% | 15\% |

